

# A Lightweight Contextual Arithmetic Coder for On-Board Remote Sensing Data Compression

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**Abstract**—The Consultative Committee for Space Data Systems (CCSDS) has issued several data compression standards devised to reduce the amount of data transmitted from satellites to ground stations. This paper introduces a contextual arithmetic encoder for on-board data compression. The proposed arithmetic encoder checks the causal adjacent neighbors, at most, to form the context and uses only bitwise operations to estimate the related probabilities. As a result, the encoder consumes few computational resources, making it suitable for on-board operation. Our coding approach is based on the prediction and mapping stages of CCSDS-123 lossless compression standard, an optional quantizer stage to yield lossless or near-lossless compression and our proposed arithmetic encoder. For both lossless and near-lossless compression, the achieved coding performance is superior to that of CCSDS-123, M-CALIC, and JPEG-LS. Taking into account only the entropy encoders, fixed-length codeword is slightly better than MQ and interleaved entropy coding.

**Index Terms**—Arithmetic coding, Consultative Committee for Space Data Systems (CCSDS)-123, lossless and near-lossless coding, remote sensing data compression.

## I. INTRODUCTION

REMOTE sensing imagery is becoming an invaluable tool for governments, rescue teams, and aid organizations to manage infrastructure and natural resources, to appraise climate changes, or to give support when natural disasters strike. Since remote sensing images tend to be very large, high-performance compression techniques are of paramount importance.

Let  $I$ ,  $J$ , and  $K$  be the number of columns, rows, and components of an image  $x$  and let  $x_{i,j,k}$  denote a pixel at location  $(i, j, k)$  of the image. Such an image is commonly compressed employing one of three regimes: lossless compression, which allows perfect reconstruction of the original image  $x$ ; lossy compression, which approximates  $x$ , introducing an error in

the reconstructed image  $x'$  that enables a higher compression ratio than possible with lossless compression; or near-lossless compression, which is a particular case of lossy compression where the peak absolute error (PAE) of  $x'$  is controlled during the coding process with a tolerance value  $\Delta$ . Specifically

$$\max_{i,j,k} \{|x_{i,j,k} - x'_{i,j,k}|\} \leq \Delta. \quad (1)$$

Within the Consultative Committee for Space Data Systems (CCSDS) [1], the Multispectral and Hyperspectral Data Compression Working Group is in charge of proposing techniques for remote sensing data compression. Such techniques are mainly developed to be implemented on board, where limited resources are available and low complexity encoders are needed. In 1997, the CCSDS published CCSDS-121.0-B-1 [2], aimed at lossless data compression. In 2005, the CCSDS published CCSDS-122.0-B-1 [3], devised for lossless and lossy compression of monocomponent images based on wavelet transforms. In 2012, the CCSDS published its latest standard, CCSDS-123.0-B-1 [4], focused on lossless compression for multispectral and hyperspectral images based on prediction. Note that to date, there is no CCSDS standard proposal devised to multispectral and hyperspectral images for near-lossless coding. In what follows, we will refer to CCSDS-123.0-B-1 as CCSDS-123.

Lossless and near-lossless coding is an active research topic, as witnessed by the number of recent publications in the last decade [5]–[17]. Some of these contributions, such as [7], [11], and [15]–[17], yield better coding performance than CCSDS-123 for lossless compression but at the expense of an increased computational complexity. Among them, the results provided in [7] can be misleading, since they were obtained using images from the 1997 AVIRIS products, which are known to have undergone an inappropriate calibration [18]. Next three contributions [11], [15], and [16] yield better coding performance than CCSDS-123, but at the expense of an increased computational complexity due to the expensive algorithms applied to improve prediction estimation. The last contribution [17] yields competitive coding performance by including a light spectral regression in the spectral domain, which has a low computational cost.

It is worth noting that none of the previous techniques provides support for near-lossless coding, which is demanded if even better coding performance is requested. Near-lossless coding [5], [6], [8]–[10], [12]–[14] can yield higher compression ratios at a bounded distortion of  $\Delta > 0$ . Some of the most

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79 prominent recent contributions for near-lossless compression  
 80 are [12], which presents an overview of the latest coding  
 81 standards for remote sensing, including a near-lossless version  
 82 of CCSDS-123; [8] and [9], which introduce a near-lossless  
 83 coding based on wavelet transforms; [14], which goes one step  
 84 further, proposing an embedded near-lossless coding system  
 85 based on wavelet transform and prediction coding; and [13],  
 86 which presents a rate control method for predictive image  
 87 encoders using the CCSDS-123 predictor. Most of the latest  
 88 contributions use the CCSDS-123 predictor, since it is suitable  
 89 for being used on board thanks to its low complexity and high  
 90 decorrelation efficiency.

91 After the predictor of CCSDS-123, one can choose between  
 92 a sample- or a block-adaptive encoder. The sample-adaptive  
 93 encoder achieves better performance than the block-adaptive  
 94 encoder when the signal is encoded at more than 1 b/sample.  
 95 However, because the minimum codeword length of the  
 96 sample-adaptive encoder is 1 b, block-adaptive encoding yields  
 97 superior performance for signals that can be encoded at less  
 98 than 1 b/sample.

99 Although context-based arithmetic encoders typically obtain  
 100 excellent coding performance at all rates, they are not included  
 101 in CCSDS-123 because they can have a high computa-  
 102 tional demand owing to: 1) probability estimation; 2) the  
 103 renormalization procedure; and 3) context formation, which  
 104 are expensive operations and are executed intensively.  
 105 Despite the computational demand of context-based arithmetic  
 106 encoders, they are included in some remote sensing coding  
 107 approaches [6], [19], [20]. Contributions aimed to reduce  
 108 the computational load by estimating the probability using  
 109 multiplication-free implementations can be found in the liter-  
 110 ature: the Q coder [21] approached the interval division  
 111 by means of lookup tables and the M coder [22] uses a  
 112 reduced range of possible subinterval sizes together with  
 113 lookup tables. Some methods based on these approaches  
 114 have been introduced in different standards [23]–[26]. The  
 115 operations carried out by the renormalization procedure can  
 116 be avoided if, instead of producing a single codeword, the  
 117 coder produces short codewords of fixed length [27], [28].  
 118 In particular, [28] presents a context-adaptive binary arithmetic  
 119 coder with fixed-length coderwords (FLWs) that outperforms  
 120 the MQ [29] and M coders in terms of coding performance.  
 121 FLW avoids the renormalization procedure but still estimates  
 122 probabilities through the division.

123 It is worth noting that none of the previously mentioned  
 124 contributions is devised to reduce the computation related to  
 125 probability estimation and the renormalization simultaneously.  
 126 In this paper, we propose an arithmetic encoder that: 1) utilizes  
 127 inexpensive operations to estimate probabilities; 2) does not  
 128 incorporate the renormalization procedure; and 3) employs a  
 129 simple context model. It yields strong coding performance at  
 130 low and high rates for remote sensing images. Our probability  
 131 estimation procedure builds on that of FLW. Originally, FLW  
 132 uses a sliding window to estimate the probability of the  
 133 symbols coded using a division operation. Herein, the sliding  
 134 window size of FLW is adapted to deal only with power of  
 135 two sizes, which allows the use of low-complexity bitwise  
 136 operations and spares the division.



Fig. 1. CCSDS-123 encoding scheme.

137 The proposed arithmetic coder is incorporated in a lossless  
 138 and near-lossless coding scheme, providing improved com-  
 139 pression performance over current remote sensing image com-  
 140 pression techniques. Roughly described, the adopted coding  
 141 scheme departs from the predictor and mapping included in  
 142 CCSDS-123 and utilizes a near-lossless quantizer, employs a  
 143 binary arithmetic coder that operates on a line-by-line and  
 144 bitplane-by-bitplane basis, introduces a new context model that  
 145 evaluates (at most) only causal adjacent samples, and uses only  
 146 bitwise operations to estimate symbol probabilities. Extensive  
 147 experimental results indicate that our proposed approach  
 148 improves on CCSDS-123 in terms of lossless compression  
 149 ratios and also outperforms a near-lossless version of the  
 150 sample-adaptive and block-adaptive coders of CCSDS-123,  
 151 JPEG-LS [30] and M-CALIC [6] in terms of lossless and near-  
 152 lossless coding performances. Comparing only the entropy  
 153 encoders, FLW is slightly better than MQ and interleaved  
 154 entropy coder (IEC) [31].

155 The rest of this paper is structured as follows. Section II  
 156 briefly reviews the CCSDS-123 coding system and a near-  
 157 lossless technique for coding systems based on prediction.  
 158 Section III describes our proposed context-based arithmetic  
 159 coder with bitwise probability estimation. Section IV describes  
 160 how our proposed arithmetic coder is incorporated in a coding  
 161 scheme that uses the predictor of CCSDS-123. Section V  
 162 presents the experimental results. Section VI concludes this  
 163 paper.

## 164 II. CCSDS-123 AND NEAR-LOSSLESS COMPRESSION

### 165 A. CCSDS-123

166 The CCSDS-123 standard, which is limited to encoding  
 167 samples of  $N = 16$  b/pixel/band, can be structured in three  
 168 stages: *predictor*, *mapper*, and *entropy encoder*. Fig. 1 illus-  
 169 trates the encoding pipeline of CCSDS-123.

170 In summary, the predictor estimates the value of the current  
 171 sample  $x_{i,j,k}$  using previously scanned samples. This predicted  
 172 sample is denoted by  $\tilde{x}_{i,j,k}$ . The prediction error  $\Lambda$  is com-  
 173 puted as

$$174 \Lambda_{i,j,k} = x_{i,j,k} - \tilde{x}_{i,j,k} \quad (2)$$

175 and then mapped to a non-negative integer  $\lambda_{i,j,k}$  called the  
 176 mapped prediction residual. The entropy encoder is in charge  
 177 of encoding  $\lambda_{i,j,k}$  without loss. For the entropy encoder in  
 178 CCSDS-123, one can choose between a sample- and a block-  
 179 adaptive encoder.

180 Further details of the CCSDS-123 stages can be found  
 181 in [12] and [32].

### 182 B. Near-Lossless Compression

183 For the encoder described above, the decoder can reproduce  
 184  $x_{i,j,k}$ , without loss. In this section, we discuss the addition of a

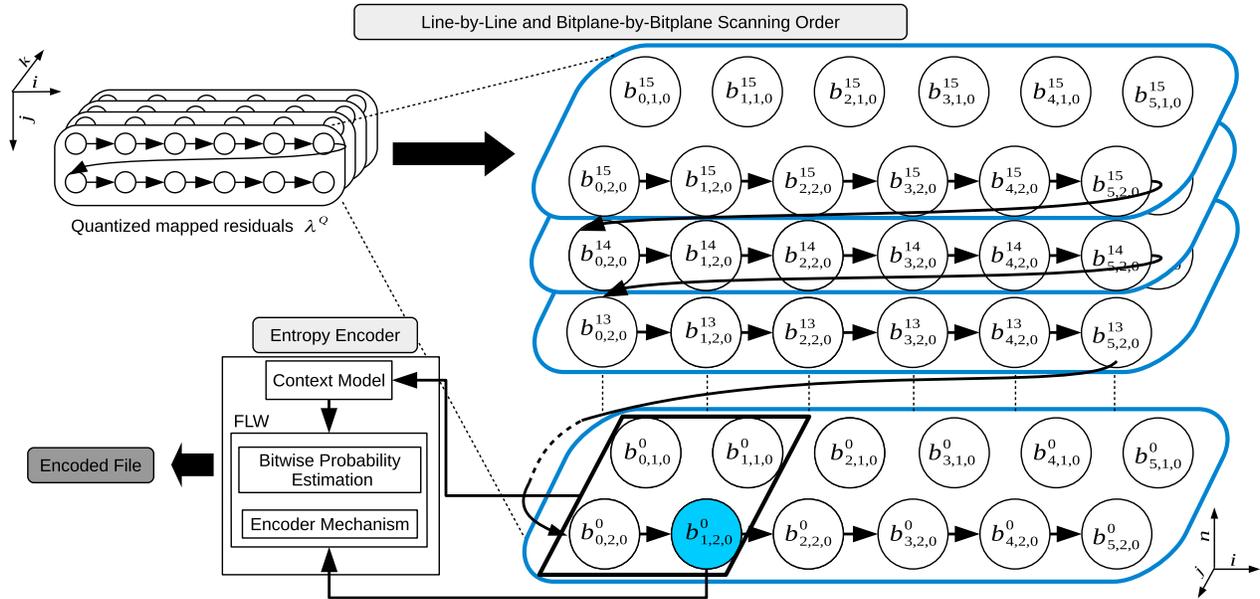


Fig. 2. Illustration of the scanning order and the entropy encoder.

185 quantizer, which results in higher compression ratios, but at the  
 186 expense of some loss of fidelity in the decompressed image.  
 187 The simplest and most effective way to design a  
 188 prediction-based lossy compression algorithm is to quantize  
 189 the prediction error  $\Lambda_{i,j,k}$  with a quantizer  $Q$ , resulting  
 190 in quantized-then-dequantized version  $\hat{\Lambda}_{i,j,k}$  (and, in conse-  
 191 quence,  $\hat{\lambda}_{i,j,k}$ ). The resulting quantization index is referred  
 192 to as  $\Lambda_{i,j,k}^Q$  and its remapped version is denoted by  $\lambda_{i,j,k}^Q$ .  
 193 Subsequent predictions  $\tilde{x}_{i,j,k}$  are calculated using previous  
 194 reconstructed (lossy) samples  $\hat{x}_{i,j,k}$ , which are obtained by  
 195 implementing a decoder in the encoder [12], [33]. The decoder  
 196 creates the reconstructed (lossy) image samples via

$$\hat{x}_{i,j,k} = \hat{\Lambda}_{i,j,k} + \tilde{x}_{i,j,k}. \quad (3)$$

198 It is worth noting that the errors in the reconstructed pixels  
 199 are identical to the errors introduced in the prediction errors  
 200 by the quantizer. That is,  $x_{i,j,k} - \hat{x}_{i,j,k} = \Lambda_{i,j,k} - \hat{\Lambda}_{i,j,k}$ . Thus,  
 201 the errors in reconstructed pixels can be precisely controlled  
 202 by controlling the individual quantization errors. This is the  
 203 basis of “near-lossless compression.”

### 204 III. LIGHTWEIGHT BINARY ARITHMETIC CODER 205 WITH CONTEXT MODEL

206 The entropy encoder presented in this paper works with  
 207 binary symbols. To this end, we denote the  $n$ th bit of the  
 208 binary representation of  $\lambda_{i,j,k}^Q$  by  $b_{i,j,k}^n$ , with  $N-1 \geq n \geq 0$ .  
 209 Here,  $N$  is chosen to provide a sufficient number of bits to  
 210 represent all the  $\lambda_{i,j,k}^Q$ , being  $b_{i,j,k}^{N-1}$  the most significant bit.

211 To facilitate use with on-board sensors, our proposal  
 212 processes data in a line-by-line fashion. Once a line is scanned,  
 213 predicted, and mapped to positive values, it is entropy encoded  
 214 on a bitplane-by-bitplane basis. The entropy encoder makes  
 215 use of context model patterns obtained using a context window  
 216 that contains symbols coded previously to the current symbol.

217 The top left of Fig. 2 displays the quantized and remapped  
 218 prediction residuals  $\lambda^Q$ . The binary representation of these  
 219 samples is shown on the right, while the bottom left portrays  
 220 the entropy encoder, which is fed by the current bit to be  
 221 encoded and its context. The bit to be encoded is shaded in  
 222 blue, while the context window is framed with a rectangle.

#### 223 A. Context Model

224 Let  $\mathbf{M}$  be the set of all possible patterns that can occur  
 225 within the context window, with context  $m \in \mathbf{M}$  being a  
 226 particular realization, resulting in a context index  $c \in \mathbf{C} =$   
 227  $\{0, \dots, C-1\}$ . These context indices (loosely referred to  
 228 as contexts in what follows) are determined by a modeling  
 229 function  $F: \mathbf{M} \rightarrow \mathbf{C}$ . For each bit  $b$  to be coded, a probability  
 230 model is used, corresponding to its context  $c$ . In particular,  
 231 the probability model estimates the conditional probability  
 232  $p(b|c) = p(b|F(m))$ . After encoding, the probability model is  
 233 updated with the latest coded bit  $b$ . That is,  $p(b|c)$  is estimated  
 234 on the fly. Specifically, our probability model estimates the  
 235 probability  $p(b=0|c)$ . A careful design of the context  
 236 model is required to obtain high coding efficiency. This task is  
 237 complicated by the goal of achieving low encoder complexity  
 238 for the purpose of operating on onboard remote sensing  
 239 scenarios.

240 A simple strategy for context modeling employs a context  
 241 window that contains only the three nearest causal neighbors  
 242 as depicted in Fig. 2. We consider several choices for the  
 243 context modeling function  $F$ . The first ignores all samples  
 244 within the context window except the one directly above the  
 245 sample of interest. This is indicated in Fig. 3(a). Three other  
 246 choices are shown in Fig. 3(b)–(d). The notations V, H, HV,  
 247 and HVD are used in Fig. 3, where V (vertical) denotes the  
 248 sample above the bit to be encoded, H (horizontal) denotes  
 249 the sample to the left, and D (diagonal) denotes the sample to

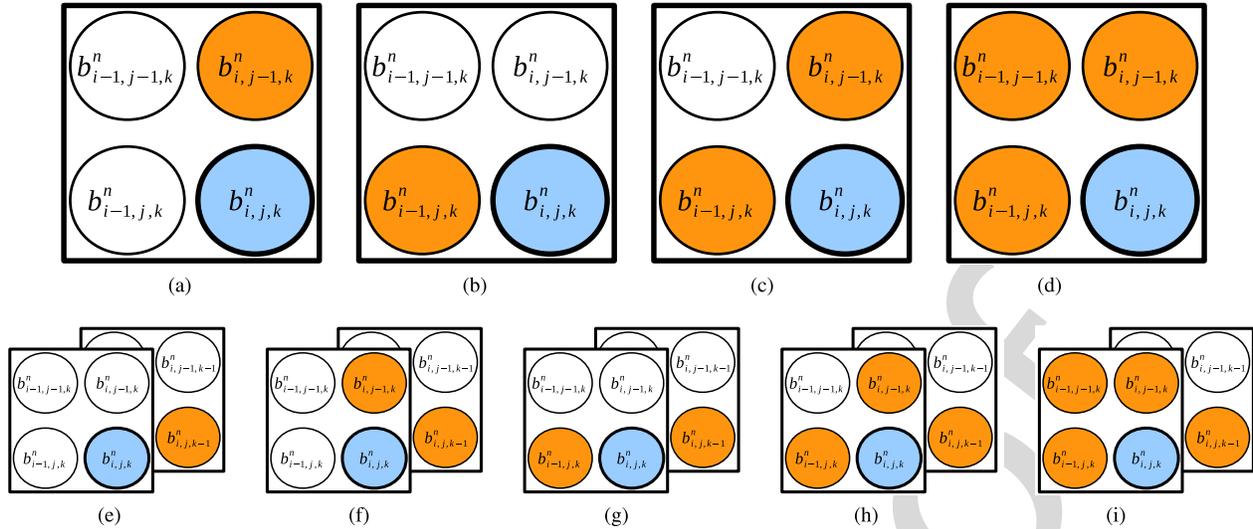


Fig. 3. Illustration of different context models to encode  $b_{i,j,k}^n$ . (a) V. (b) H. (c) HV. (d) HVD. (e) S. (f) VS. (g) HS. (h) HVS. (i) HVDS.

TABLE I  
CONTEXT ASSIGNMENTS FOR THE V, H, HV, AND HVD MODELING FUNCTIONS

$c$	V	H	HV		HVD		
	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i-1,j-1,k}^n$
0	0	0	0	0	0	0	0
1	1	1	0	1	0	0	1
2			1	0	0	1	0
3			1	1	0	1	1
4					1	0	0
5					1	0	1
6					1	1	0
7					1	1	1

the left and above. To take advantage of dependencies between spectral components, the preceding spectral component  $k-1$  can be included in the context window. In this case, S (spectral) denotes the coregistered sample in the previous spectral component. The inclusion of this sample gives rise to five additional modeling functions as shown in Fig. 3(e)–(i). Note that if only samples H and S are employed by the modeling function, only the current scanned line must be stored in memory. For all other modeling functions, the previous and the current lines are necessary.

Rather than the actual bit (from bitplane  $n$ ) of each neighboring sample, the so-called “significance state” is employed to compute the context  $c$ . To this end, let  $s_{i,j,k}^n$  denote the significance state of the sample at location  $i, j, k$  at bitplane  $n$ . A value of 1 indicates that the sample contains a 1 at bitplane  $n$  or higher. Table I shows how  $c$  is derived from the significance states of the neighbors for the V, H, HV, and HVD modeling functions. The S modeling function results in two states, i.e.,  $c \in \{0, 1\}$ . The VS, HS, HVS, and HVDS modeling functions result in twice the number of states than their counterparts that do not employ S. They are not shown in Table I for the sake of space. The experimental results for all context modeling functions are presented in a subsequent section.

Before finishing this section, we note that the entropy coder and its associated probability models are initialized at the

beginning of each bit plane of each component. In particular, the initial probability model for each context is set to a value of  $p(b=0|c) = 0.66$ . The probability is biased toward 0 since, as found empirically, bits of higher bitplanes have higher probability of being 0, thus allowing FLW to adapt faster. This, together with the fact that all bitplane data from the current line (and its predecessor, when relevant) are available in the encoder, leads to the conclusion that the bitplanes of the current line can be encoded in parallel. This parallel strategy is not possible in the decoder. The use of significant states in the context formation process requires that bitplanes be decoded sequentially. We note that the probabilities are reset ( $p(b=0|c) = 0.66$ ) at the beginning of each component without penalizing the coding performance. This is because only  $2^{12}$  symbols are encoded with the default probability value, which on average for the image corpora used, corresponds to the 0.06% of the total symbols per band to be encoded.

### B. Bitwise Probability Estimation

As mentioned before, FLW was devised to reduce computational costs through the use of FLWs, which avoids a renormalization operation, but is not aimed to reduce the computational load derived from probability estimation [28].

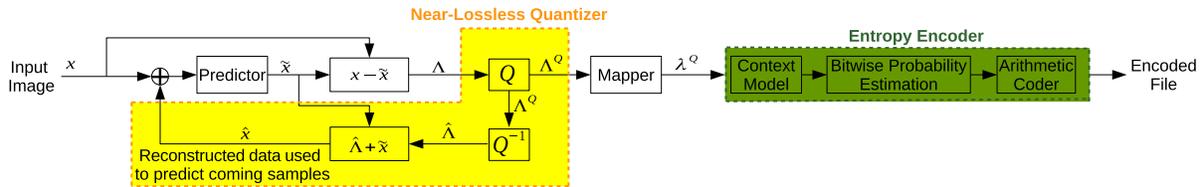


Fig. 4. Adopted coding approach.

 TABLE II  
 MAIN DIFFERENCES BETWEEN CCSDS-123 AND THE ADOPTED APPROACH

	Predictor	Quantizer	Mapper	Data Scanned Supported	Context Model	Entropy Encoder
CCSDS-123	✓	✗	✓	Line or Block	✗	Sample-Adaptive or Block-Adaptive
Proposal	✓	✓	✓	Line	✓	Contextual Binary Arithmetic Coder

For each context  $c$ , FLW uses a sliding window of symbols coded with that context. The length of this window varies between  $\mathcal{T}$  and  $2\mathcal{T} - 1$  symbols. The probability estimate is updated once every  $\mathcal{V}$  symbols coded, according to

$$p(b = 0|c) = \frac{Z \lll \mathcal{B}}{W} \quad (4)$$

with  $W$  representing the number of symbols within the window,  $Z$  the number of zeroes within the window, and  $\mathcal{B}$  the number of bits used to express symbol probabilities. The numerator of the expression is computed by left shifting the binary representation of  $Z$  by  $\mathcal{B}$  bits. The size of the window is incremented each time a symbol is encoded using context  $c$  until  $W = 2\mathcal{T}$ , at which time the window size is immediately reduced to  $\mathcal{T}$  and the number of zeroes within the window is updated according to  $Z \leftarrow Z - Z'$  and  $Z' \leftarrow Z$ , with  $Z'$  being the number of zeroes coded during the most recent  $\mathcal{T}$  symbols.

In the original approach of FLW as formulated above,  $p(b|c)$  is computed via a division operation to achieve maximum accuracy. Such a division may tax the on-board computational resources in a remote sensing scenario. To reduce computational complexity, we propose to estimate the probability through bitwise operations. The substitution of the division by bitwise operations requires that  $\mathcal{V} = \mathcal{T}$  and that both are a power of two. This forces the sliding window to contain a power of two symbols, so the probability can be updated using only bit shift operations according to

$$p(b|c) = (Z \lll \mathcal{B}) \ggg \log_2(W) \quad (5)$$

where  $W$  and  $Z$  are then updated through  $W \leftarrow W \ggg 1$  and  $Z \leftarrow Z \ggg 1$ . Note that this update rule for  $Z$  approximates only the number of zeroes in the most recent  $\mathcal{T}$  coded samples. Nevertheless, the update can be carried out in the decoder using the same approximation. At the beginning of encoding, the probability is first updated when  $\mathcal{V}$  symbols are coded. Subsequently, it is updated every  $\mathcal{V}/2$  symbols. The strategy proposed here can be seen as a special case of (4), which was not explored in [28].

Using (5) instead of (4) reduces the flexibility of the arithmetic coder since the updating of the probability estimates and the window size are tied together. The maximum performance

achieved with the original formulation of the arithmetic coder proposed in [28] is achieved when the probability estimate is updated every symbol, i.e.,  $\mathcal{V} = 1$ , regardless of the window size. The strategy proposed here provides a significant reduction in complexity with a minor reduction in compression performance. The experimental results provided in Section V indicate that our approach yields highly competitive compression performance.

#### IV. ADOPTED CODING APPROACH

Although the novel entropy encoder presented here may be incorporated in any coding system, we employ it in the CCSDS-123 coding pipeline. Fig. 4 illustrates the adopted coding approach, which employs the predictor and mapper of CCSDS-123, but adds a near-lossless quantizer (see the yellow block), and substitutes the usual CCSDS-123 encoder by our entropy encoder (see the green block). The circle containing a cross at the left side of Fig. 4 indicates that the input to the predictor is either the original pixel  $x$  (when the optional quantization is not present) or the reconstructed pixel  $\hat{x}$  (when quantization is present).

The adopted coding scheme is evaluated with a uniform quantizer (UQ) and a uniform scalar deadzone quantizer (USDQ) [29]. The UQ operates over  $\Lambda_{i,j,k}$  to obtain a quantization index according to

$$\Lambda_{i,j,k}^Q = \text{sign}(\Lambda_{i,j,k}) \left\lfloor \frac{|\Lambda_{i,j,k}| + \Delta}{2\Delta + 1} \right\rfloor \quad (6)$$

where  $2\Delta + 1$  is the quantization step size. The operation to reconstruct  $\hat{\Lambda}_{i,j,k}$  from its quantization index is given by

$$\hat{\Lambda}_{i,j,k} = \text{sign}(\Lambda_{i,j,k}^Q) (2\Delta + 1) \Lambda_{i,j,k}^Q. \quad (7)$$

The UQ is employed in lossless compression techniques such as JPEG-LS, M-CALIC, and 3-D-CALIC [34]. On the other hand, the USDQ quantizes  $\Lambda_{i,j,k}$  to obtain a quantization index according to

$$\Lambda_{i,j,k}^Q = \text{sign}(\Lambda_{i,j,k}) \left\lfloor \frac{|\Lambda_{i,j,k}|}{\Delta + 1} \right\rfloor \quad (8)$$

TABLE III

SUMMARY OF DATA USED IN THE EXPERIMENTAL RESULTS. SENSOR NAME, ITS ABBREVIATION, THE NUMBER OF IMAGES FROM EACH SENSOR, AND FIRST-ORDER ENTROPIES (IN BITS PER SAMPLE) ON AVERAGE PER SENSOR ARE PROVIDED. THE LAST TWO COLUMNS INDICATE THE PREDICTOR MODE AND THE LOCAL SUM USED FOR EACH SENSOR

Sensor	Abbreviation	Number of images	Entropy	Predictor Mode	Local Sum
Aviris Calibrated	AC	5	9.77	Neighbor Oriented	Full Mode
Aviris Uncalibrated	AU	7	11.21	Neighbor Oriented	Full Mode
Airs	A	9	11.34	Neighbor Oriented	Reduced Mode
Casi	C	2	10.52	Neighbor Oriented	Reduced Mode
Crism	Cr	20	10.69	Column Oriented	Reduced Mode
Hyperion	H	4	9.53	Column Oriented	Reduced Mode
M3	M3	5	9.19	Column Oriented	Reduced Mode
Total / average	—	52	10.41	—	—

where the quantization step is  $\Delta + 1$ . The operation to reconstruct  $\hat{\Lambda}_{i,j,k}$  from its quantization index is expressed as

$$\hat{\Lambda}_{i,j,k} = \text{sign}(\Lambda_{i,j,k}^Q)(\Delta + 1)\Lambda_{i,j,k}^Q. \quad (9)$$

Due to its straightforward implementation and excellent performance, the USDQ has been selected for the JPEG 2000 standard [24]. The USDQ partitions the range of input values into intervals all of size  $\Delta$ , except for the interval that contains zero, which is of size  $2\Delta$ . This results in all absolute pixel errors  $|x_{i,j,k} - \hat{x}_{i,j,k}|$  being bounded above  $\Delta$  for both quantizers.

Table II summarizes the main differences between CCSDS-123 and the adopted coding scheme.

## V. EXPERIMENTAL RESULTS

This section presents a set of experiments aimed at the analysis and evaluation of the adopted coding scheme. First, the proposed context modeling functions are evaluated in terms of the conditional entropy of the prediction residual. The bitwise probability estimator is then evaluated via the same performance metric to determine its proper configuration. A variety of binary encoder mechanisms such as IEC, MQ, and FLW are evaluated in terms of their lossless compression performance in conjunction with the proposed context modeling and probability estimation. Finally, the resulting proposed overall approach is compared in terms of lossless and near-lossless compression performances with CCSDS-123, JPEG-LS, and M-CALIC.

For the experiments conducted in this paper, we have selected a set of images<sup>1</sup> collected with different sensors that are included in CCSDS MHDC-WG corpus. The sensor names and their main features are listed in Table III. The average entropy is reported for each image type. The reported values are first-order entropy; they represent the entropy of individual pixels, without accounting for any dependencies among pixels within or between components.

In [35], the impact of different CCSDS-123 parameters that control the operation of the prediction and the entropy encoder was evaluated, suggesting that a correct parameter

selection had more impact on the predictor stage than in the entropy encoder stage. Concerning the prediction, the parameters local sum type, prediction mode, the number of prediction bands, and predictor adaption rate were the most critical. Extensive experimental evaluations were conducted to find suitable configurations.

In this paper, leaning on the results in [35] and after conducting an extensive evaluation also, experimental results are produced for the following parameter configuration: the local sum type and predictor mode depend on the acquisition sensor (as indicated in the last two columns of Table III); the number of prediction bands  $P$  is set to 3, since it is a good tradeoff between the computational load and the coding performance; and the predictor adaptation rate  $v_{\max}$  is set to 3, since, in general, it yields the best performance.

For evaluating the performance of context modeling and probability estimation, we employ the conditional entropy of the prediction residuals, as mentioned above. For the work proposed here, binary entropy coding is employed. To yield results with units in bits per pixel, the binary entropies of all bitplanes are added. Since our context model estimates the probability of  $p(b = 0|c)$ , the conditional entropy of an image (in bits) is computed as

$$H(\lambda^Q) = \sum_{i=0}^{I-1} \sum_{j=0}^{J-1} \sum_{k=0}^{K-1} \sum_{n=0}^{15} \times \begin{cases} \log_2(p(b_{i,j,k}^n = 0|c)) & \text{if } b_{i,j,k}^n = 0 \\ \log_2(1 - p(b_{i,j,k}^n = 0|c)) & \text{if } b_{i,j,k}^n = 1 \end{cases} \quad (10)$$

where  $\lambda^Q$  denotes the symbols to be entropy coded.

### A. Context Modeling Function

The context model is used to select the probability model that is employed to encode the current symbol. In this first experiment, each of the probability models themselves is estimated using the high-performance method given by (4) employing  $\mathcal{V} = 1$  and  $\mathcal{T} = 2^{12}$ , without regard to complexity.

Table IV provides the conditional entropy obtained (in bits per sample) for the different context formations defined in Section III-A, i.e., V, H, HV, HVD, S, VS, HS, HVS, and HVDS. The results from Table III suggest the following.

<sup>1</sup>The images used are available at <http://cwe.ccsds.org/sls/docs/sls-dc/123.0-B-Info/TestData>

TABLE IV

CONDITIONAL ENTROPY OF THE PREDICTION RESIDUALS (IN BITS PER SAMPLE) FOR THE CONTEXT MODELING FUNCTIONS DENOTED BY V, H, HV, HVD, S, VS, HS, HVS, AND HVDS. RESULTS ARE REPORTED ON AVERAGE FOR DIFFERENT SENSORS AND  $\Delta = 0$

Sensor	Context Formation								
	V	H	HV	HVD	S	VS	HS	HVS	HVDS
AC	3.69	3.69	3.68	3.68	3.69	3.68	3.68	3.68	3.67
AU	5.01	5.00	5.00	4.99	5.00	4.99	4.99	4.99	4.99
A	4.24	4.23	4.24	4.24	4.24	4.24	4.24	4.24	4.23
C	4.85	4.85	4.84	4.84	4.85	4.84	4.84	4.83	4.83
Cr	4.15	4.21	4.14	4.14	4.20	4.12	4.19	4.12	4.12
H	4.26	4.26	4.25	4.25	4.29	4.26	4.26	4.25	4.25
M3	2.66	2.70	2.65	2.65	2.70	2.64	2.68	2.63	2.63
Average	4.12	4.14	4.11	4.11	4.14	4.11	4.13	4.10	4.10

TABLE V

CONDITIONAL ENTROPY OF THE PREDICTION RESIDUALS (IN BITS PER SAMPLE) FOR  $\Delta = 0$  RESULTING FROM THE MAXIMUM PRECISION AND THE BITWISE PROBABILITY ESTIMATORS. THE V CONTEXT MODEL IS EMPLOYED IN EACH CASE. THE BEST RESULTS FOR EACH STRATEGY ARE REPRESENTED IN BOLD

$\mathcal{T} =$	division $\mathcal{V} = 1$					bitwise operations $\mathcal{V} = \mathcal{T}$				
	$2^{16}$	$2^{14}$	$2^{12}$	$2^{10}$	$2^8$	$2^{16}$	$2^{14}$	$2^{12}$	$2^{10}$	$2^8$
	AC	3.70	3.69	<b>3.69</b>	3.70	3.75	3.72	3.70	<b>3.69</b>	3.70
AU	5.02	5.01	<b>5.01</b>	5.01	5.06	5.04	5.02	<b>5.01</b>	5.02	5.08
A	4.27	4.26	<b>4.23</b>	4.24	4.26	4.32	4.29	<b>4.24</b>	4.26	4.28
C	4.94	4.86	<b>4.85</b>	4.86	4.89	4.90	4.86	<b>4.85</b>	4.86	4.91
Cr	4.16	4.15	<b>4.15</b>	4.15	4.18	4.21	4.17	<b>4.16</b>	4.16	4.20
H	4.27	4.26	<b>4.26</b>	4.27	4.31	4.29	4.27	<b>4.26</b>	4.27	4.32
M3	2.69	2.66	<b>2.66</b>	2.67	2.70	2.71	2.68	<b>2.67</b>	2.68	2.72
Average	4.15	4.13	<b>4.12</b>	4.13	4.16	4.17	4.14	<b>4.13</b>	4.13	4.18

- 1) All of the modeling functions provide significant improvements over the pixel entropy reported in Table III.
  - 2) The differences in performance between the modeling functions are generally small.
  - 3) Although the context models H and S yield the worst performance on average, they are the best option when memory resources are severely limited since they need only to store samples from the current line to be encoded.
  - 4) Adding the S sample to a context results in an improvement of only about 0.01 b/sample.
  - 5) The V context obtains a coding benefit of 0.02 b/sample on average with respect to the H context and only adds the previous processed line to its storage requirements.
- In what follows, we select context model V for further evaluation due to its favorable tradeoff among the performance, memory resources, and computational load.

estimation strategies. In both cases, the V context model is employed. The left of Table V presents results for the maximum precision technique (using division), as defined by (4). These results are shown for different values of  $\mathcal{T}$ , but  $\mathcal{V} = 1$ . The right side of Table V presents results for the bitwise strategy, as defined by (5). The same values of  $\mathcal{T}$  are explored, but always with  $\mathcal{V} = \mathcal{T}$ , as required to avoid division. The results suggest that  $\mathcal{T} = 2^{12}$  attains the highest performance for both strategies. A larger  $\mathcal{T}$  degrades the coding performance because the window may contain symbols that are not correlated with the current one. A smaller  $\mathcal{T}$  degrades the coding performance because there are insufficient symbols to reliably estimate the probabilities  $p(b|C)$ . The results of Table V also indicate that the low-complexity strategy that employs bitwise operations is as competitive as that employing division. Although not tabulated here for the sake of space, these results hold for the other context modeling functions considered in the previous sections.

**B. Probability Estimation**

This section reports the results obtained by the two different probability estimation strategies discussed in Section III. In particular, Table V reports the conditional entropy of the prediction residuals resulting from the two different probability

**C. Entropy Coding**

We note that the context model and probability estimator proposed here can be used with any entropy encoder that codes binary symbols according to a given probability model, such as MQ, IEC or the adopted FLW. Table VI provides the actual

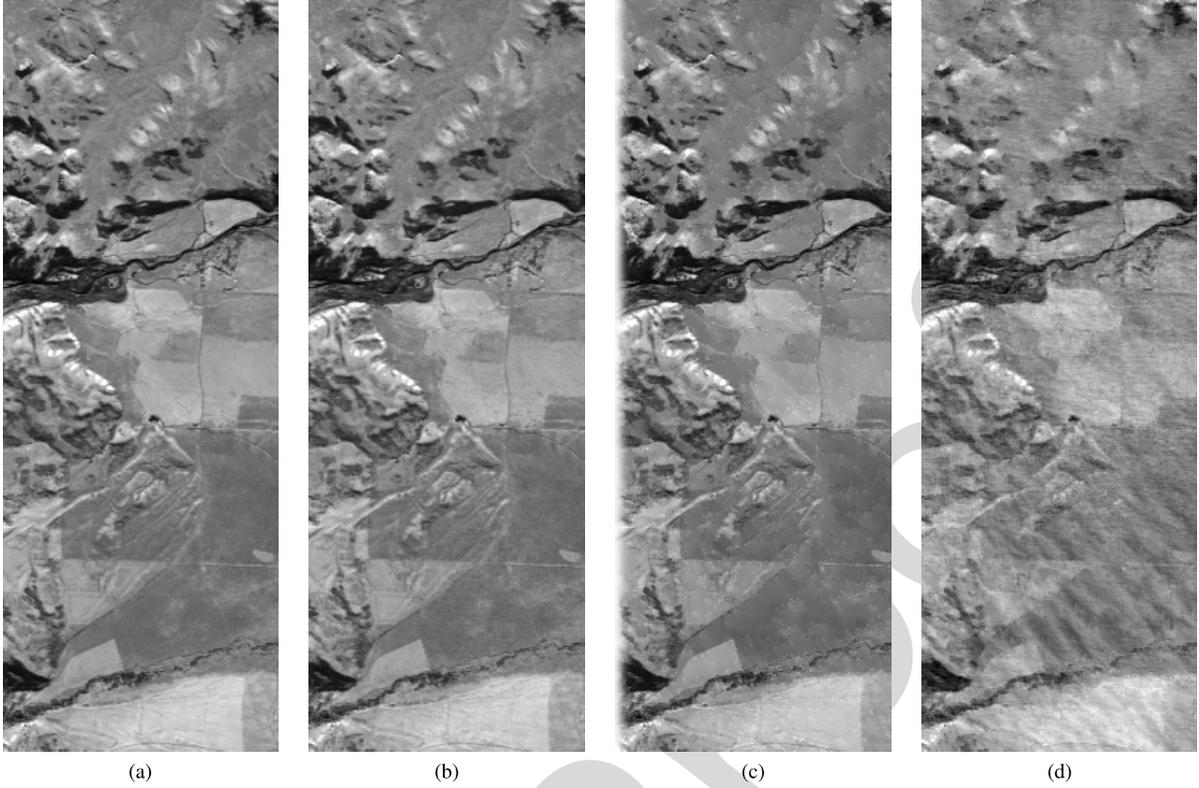


Fig. 5. Visual comparison for the “Avisis Calibrated Yellowstone sc00” image. (a) Original. (b) Proposed approach at 0.43 b/sample ( $\Delta = 20$ ). (c) M-CALIC at 0.42 b/sample ( $\Delta = 30$ ). (d) CCSDS-123 at 0.50 b/sample ( $\Delta = 80$ ).

TABLE VI  
CODING PERFORMANCE (IN Bits per Sample) OF THE PROPOSED  
APPROACH USING MQ, IEC, AND FLW ENTROPY ENCODING.  
ALL RESULTS EMPLOY CONTEXT MODEL V AND BITWISE  
PROBABILITY ESTIMATION WITH  $T = \mathcal{V} = 2^{12}$

Sensor	MQ	IEC	FLW
AC	3.74	3.72	3.71
AU	5.06	5.04	5.03
A	4.30	4.29	4.28
C	4.90	4.88	4.87
Cr	4.20	4.18	4.18
H	4.31	4.29	4.28
M3	2.71	2.70	2.69
Average	4.17	4.16	4.15

490 compression results (in bits per sample) obtained using the  
491 MQ, IEC, and FLW entropy coders. In each case, the results  
492 are obtained with context model V and the bitwise estimator  
493 with  $T = \mathcal{V} = 2^{12}$ . From these results, we can see that, on  
494 average, FLW yields slightly better results than IEC and MQ.

#### 495 D. Lossless and Near-Lossless Compression

496 The results reported in this section compare the loss-  
497 less performance of the proposed approach with those of  
498 JPEG-LS, M-CALIC, and CCSDS-123. Additionally, we com-  
499 pare its *near-lossless* performance with those of JPEG-LS  
500 and M-CALIC and the implementation of CCSDS-123.  
501 Different quantizers have been combined with our proposal  
502 and CCSDS-123, to obtain an as fair as possible comparison.

In particular, the UQ and the USDQ discussed in Section IV  
are compared.

M-CALIC and the near-lossless version of CCSDS-123 are  
considered to be state of the art in terms of compression  
performance and computational complexity, and JPEG-LS is a  
standard technique with near-lossless features. All results for  
the proposed scheme are produced using the FLW arithmetic  
coder, context model V, and the bitwise probability estimator  
having  $\mathcal{V} = T = 2^{12}$ . The results reported in Table VII  
indicate that our method outperforms both M-CALIC and  
CCSDS-123 in terms of lossless coding ( $\Delta = 0$ ) for all  
sensors. In the near-lossless regime ( $\Delta > 0$ ), the proposed  
approach outperforms M-CALIC when the USDQ is used and  
in most cases for the UQ. In particular, M-CALIC obtains  
slightly better results than our proposal only for images  
acquired with sensors AIRS and Hyperion when the UQ  
is used. On the other hand, the proposed system always  
outperforms the near-lossless extension of CCSDS-123 for  
both quantizers. In addition, in general, for the same  $\Delta$  value,  
the coding performance is better for the USDQ than for UQ.  
Although achieved bit rates vary widely from image to image,  
low bit rates can be obtained for all images with a modest  
value of PAEs (maximum absolute pixel error).

#### E. Visual Comparison

To evaluate visual performance, we show a region cropped  
from an image encoded at the “same” bit rate by the proposed  
approach with the UQ, M-CALIC, and CCSDS-123. For  
CCSDS-123, we employ the block-adaptive coder since we  
want to compare the images at a bit rate lower than 1 b/sample.

TABLE VII

LOSSLESS ( $\Delta = 0$ ) AND NEAR-LOSSLESS ( $\Delta > 0$ ) COMPRESSION RESULTS FOR THE PROPOSED APPROACH. FOR COMPARISON, THE RESULTS FOR JPEG-LS, M-CALIC, AND CCSDS-123 ARE INCLUDED. BOTH A UQ AND A USDQ HAVE BEEN USED IN OUR PROPOSED APPROACH AND IN OUR NEAR-LOSSLESS EXTENSION TO CCSDS-123 TO PRODUCE RESULTS FOR  $\Delta > 0$ . THE RESULTS ARE REPORTED IN BITS PER SAMPLE (LOWER IS BETTER)

Sensor	$\Delta$ values	CCSDS-123				JPEG-LS	M-CALIC	Our Proposal	
		with UQ		with USDQ				with UQ	with USDQ
		Sample adaptive	Block adaptive	Sample adaptive	Block adaptive				
AC	$\Delta = 0$	3.73	3.91	3.73	3.91	6.41	3.87	<b>3.71</b>	<b>3.71</b>
	$\Delta = 10$	1.20	0.97	1.20	0.94	2.45	0.76	<b>0.62</b>	<b>0.60</b>
	$\Delta = 20$	1.10	0.74	1.10	0.72	1.81	0.50	<b>0.38</b>	<b>0.36</b>
	$\Delta = 30$	1.07	0.64	1.07	0.63	1.48	0.40	<b>0.28</b>	<b>0.27</b>
AU	$\Delta = 0$	5.06	5.23	5.06	5.23	7.47	5.13	<b>5.03</b>	<b>5.03</b>
	$\Delta = 10$	1.69	1.68	1.85	1.78	3.41	1.46	<b>1.39</b>	1.52
	$\Delta = 20$	1.35	1.19	1.40	1.21	2.68	0.95	<b>0.87</b>	0.90
	$\Delta = 30$	1.24	0.98	1.26	0.99	2.30	0.73	<b>0.65</b>	0.67
A	$\Delta = 0$	4.29	4.48	4.29	4.48	6.85	4.28	<b>4.27</b>	<b>4.27</b>
	$\Delta = 10$	1.23	1.12	1.18	0.96	2.62	0.73	0.76	<b>0.62</b>
	$\Delta = 20$	1.10	0.75	1.07	0.65	1.86	0.41	0.39	<b>0.30</b>
	$\Delta = 30$	1.06	0.63	1.05	0.56	1.50	0.31	0.28	<b>0.22</b>
C	$\Delta = 0$	4.97	5.15	4.97	5.15	6.79	4.91	<b>4.87</b>	<b>4.87</b>
	$\Delta = 10$	1.47	1.48	1.51	1.47	2.64	1.12	<b>1.10</b>	<b>1.10</b>
	$\Delta = 20$	1.25	1.06	1.25	1.03	1.94	0.68	0.67	<b>0.64</b>
	$\Delta = 30$	1.17	0.88	1.18	0.87	1.58	0.52	0.49	<b>0.48</b>
Cr	$\Delta = 0$	4.40	4.50	4.40	4.50	5.10	6.91	<b>4.18</b>	<b>4.18</b>
	$\Delta = 10$	1.64	1.66	1.63	1.42	1.83	2.75	1.26	<b>0.99</b>
	$\Delta = 20$	1.43	1.34	1.39	1.05	1.47	2.02	0.92	<b>0.64</b>
	$\Delta = 30$	1.34	1.17	1.30	0.89	1.29	1.64	0.76	<b>0.50</b>
H	$\Delta = 0$	4.37	4.57	4.37	4.57	6.24	4.80	<b>4.28</b>	<b>4.28</b>
	$\Delta = 10$	1.38	1.45	1.21	1.08	2.74	1.02	1.06	<b>0.68</b>
	$\Delta = 20$	1.24	1.19	1.09	0.74	2.06	0.52	0.77	<b>0.35</b>
	$\Delta = 30$	1.18	1.04	1.06	0.63	1.68	0.33	0.62	<b>0.25</b>
M	$\Delta = 0$	2.81	2.97	2.81	2.97	4.24	5.18	<b>2.69</b>	<b>2.69</b>
	$\Delta = 10$	1.26	1.21	1.11	0.74	1.38	1.32	0.76	<b>0.33</b>
	$\Delta = 20$	1.17	1.01	1.07	0.60	1.20	0.78	0.56	<b>0.20</b>
	$\Delta = 30$	1.14	0.89	1.06	0.55	1.00	0.53	0.46	<b>0.15</b>
Average	$\Delta = 0$	4.23	4.40	4.23	4.40	6.16	5.01	<b>4.15</b>	<b>4.15</b>
	$\Delta = 10$	1.41	1.37	1.39	1.20	2.44	1.31	1.00	<b>0.83</b>
	$\Delta = 20$	1.23	1.04	1.20	0.86	1.86	0.84	0.65	<b>0.48</b>
	$\Delta = 30$	1.17	0.89	1.14	0.73	1.55	0.64	0.51	<b>0.36</b>

We note that none of the schemes compared here includes precise rate control. For this reason, we have employed the following methodology: 1) encode an image using a variety of different quantization step sizes for each compression scheme and 2) choose those encoded images that yield bit rates as close as possible for the three algorithms. We note that a close match was not obtained in the case of CCSDS-123, so a step size was chosen to afford a higher bit rate than that of the proposed approach, thus giving an advantage to CCSDS-123 in terms of visual performance.

The results of this process are shown in Fig. 5 for a crop from component 122 of the image “Avisis Calibrated Yellowstone sc00.” The bit rates obtained are 0.43, 0.42, and 0.50 for the proposed approach, M-CALIC, and CCSDS-123, respectively. The reader is invited to zoom in to see the specific visual artifacts arising from the different compression

schemes. Fig. 5 indicates that the image obtained by the proposed approach has higher visual quality than those by (near lossless) CCSDS-123 and M-CALIC. In particular, the proposed approach preserves edges and textures very well, while M-CALIC results in smoothness and loss of texture. CCSDS-123 also removes texture, but also introduces an annoying “banding” effect, due to the high step size required to reach 0.50 b/sample.

## VI. CONCLUSION

This paper proposes an entropy encoder based on an efficient definition for a context model and the associated strategy to estimate probabilities for use in a fixed-length arithmetic encoder using low-cost bitwise operations. These contributions are incorporated in a coding approach that employs the predictor included in CCSDS-123. A near-lossless

quantizer has also been deployed. The entropy encoder works on a line-by-line and bitplane-by-bitplane scanning order. The experimental results indicate that the use of a single neighbor for the context formation is enough to properly exploit the contextual information in the arithmetic encoder and that it is possible to estimate the probability employing bitwise operations without penalizing the coding efficiency. Further results indicate that, on average, our proposal improves the current standard version of CCSDS-123 for lossless coding by more than 0.1 b/sample. Compared with M-CALIC, our proposal provides an average improvement of 0.86 b/sample for lossless, whereas for near-lossless, the benefit ranges from 0.13 to 0.31 b/sample, depending on the allowed PAE.

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# A Lightweight Contextual Arithmetic Coder for On-Board Remote Sensing Data Compression

Joan Bartrina-Rapesta, Ian Blanes, *Senior Member, IEEE*, Francesc Aulí-Llinàs, *Senior Member, IEEE*, Joan Serra-Sagristà, *Senior Member, IEEE*, Victor Sanchez, and Michael W. Marcellin, *Fellow, IEEE*,

**Abstract**—The Consultative Committee for Space Data Systems (CCSDS) has issued several data compression standards devised to reduce the amount of data transmitted from satellites to ground stations. This paper introduces a contextual arithmetic encoder for on-board data compression. The proposed arithmetic encoder checks the causal adjacent neighbors, at most, to form the context and uses only bitwise operations to estimate the related probabilities. As a result, the encoder consumes few computational resources, making it suitable for on-board operation. Our coding approach is based on the prediction and mapping stages of CCSDS-123 lossless compression standard, an optional quantizer stage to yield lossless or near-lossless compression and our proposed arithmetic encoder. For both lossless and near-lossless compression, the achieved coding performance is superior to that of CCSDS-123, M-CALIC, and JPEG-LS. Taking into account only the entropy encoders, fixed-length codeword is slightly better than MQ and interleaved entropy coding.

**Index Terms**—Arithmetic coding, Consultative Committee for Space Data Systems (CCSDS)-123, lossless and near-lossless coding, remote sensing data compression.

## I. INTRODUCTION

REMOTE sensing imagery is becoming an invaluable tool for governments, rescue teams, and aid organizations to manage infrastructure and natural resources, to appraise climate changes, or to give support when natural disasters strike. Since remote sensing images tend to be very large, high-performance compression techniques are of paramount importance.

Let  $I$ ,  $J$ , and  $K$  be the number of columns, rows, and components of an image  $x$  and let  $x_{i,j,k}$  denote a pixel at location  $(i, j, k)$  of the image. Such an image is commonly compressed employing one of three regimes: lossless compression, which allows perfect reconstruction of the original image  $x$ ; lossy compression, which approximates  $x$ , introducing an error in

the reconstructed image  $x'$  that enables a higher compression ratio than possible with lossless compression; or near-lossless compression, which is a particular case of lossy compression where the peak absolute error (PAE) of  $x'$  is controlled during the coding process with a tolerance value  $\Delta$ . Specifically

$$\max_{i,j,k} \{|x_{i,j,k} - x'_{i,j,k}|\} \leq \Delta. \quad (1)$$

Within the Consultative Committee for Space Data Systems (CCSDS) [1], the Multispectral and Hyperspectral Data Compression Working Group is in charge of proposing techniques for remote sensing data compression. Such techniques are mainly developed to be implemented on board, where limited resources are available and low complexity encoders are needed. In 1997, the CCSDS published CCSDS-121.0-B-1 [2], aimed at lossless data compression. In 2005, the CCSDS published CCSDS-122.0-B-1 [3], devised for lossless and lossy compression of monocomponent images based on wavelet transforms. In 2012, the CCSDS published its latest standard, CCSDS-123.0-B-1 [4], focused on lossless compression for multispectral and hyperspectral images based on prediction. Note that to date, there is no CCSDS standard proposal devised to multispectral and hyperspectral images for near-lossless coding. In what follows, we will refer to CCSDS-123.0-B-1 as CCSDS-123.

Lossless and near-lossless coding is an active research topic, as witnessed by the number of recent publications in the last decade [5]–[17]. Some of these contributions, such as [7], [11], and [15]–[17], yield better coding performance than CCSDS-123 for lossless compression but at the expense of an increased computational complexity. Among them, the results provided in [7] can be misleading, since they were obtained using images from the 1997 AVIRIS products, which are known to have undergone an inappropriate calibration [18]. Next three contributions [11], [15], and [16] yield better coding performance than CCSDS-123, but at the expense of an increased computational complexity due to the expensive algorithms applied to improve prediction estimation. The last contribution [17] yields competitive coding performance by including a light spectral regression in the spectral domain, which has a low computational cost.

It is worth noting that none of the previous techniques provides support for near-lossless coding, which is demanded if even better coding performance is requested. Near-lossless coding [5], [6], [8]–[10], [12]–[14] can yield higher compression ratios at a bounded distortion of  $\Delta > 0$ . Some of the most

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79 prominent recent contributions for near-lossless compression  
 80 are [12], which presents an overview of the latest coding  
 81 standards for remote sensing, including a near-lossless version  
 82 of CCSDS-123; [8] and [9], which introduce a near-lossless  
 83 coding based on wavelet transforms; [14], which goes one step  
 84 further, proposing an embedded near-lossless coding system  
 85 based on wavelet transform and prediction coding; and [13],  
 86 which presents a rate control method for predictive image  
 87 encoders using the CCSDS-123 predictor. Most of the latest  
 88 contributions use the CCSDS-123 predictor, since it is suitable  
 89 for being used on board thanks to its low complexity and high  
 90 decorrelation efficiency.

91 After the predictor of CCSDS-123, one can choose between  
 92 a sample- or a block-adaptive encoder. The sample-adaptive  
 93 encoder achieves better performance than the block-adaptive  
 94 encoder when the signal is encoded at more than 1 b/sample.  
 95 However, because the minimum codeword length of the  
 96 sample-adaptive encoder is 1 b, block-adaptive encoding yields  
 97 superior performance for signals that can be encoded at less  
 98 than 1 b/sample.

99 Although context-based arithmetic encoders typically obtain  
 100 excellent coding performance at all rates, they are not included  
 101 in CCSDS-123 because they can have a high computa-  
 102 tional demand owing to: 1) probability estimation; 2) the  
 103 renormalization procedure; and 3) context formation, which  
 104 are expensive operations and are executed intensively.  
 105 Despite the computational demand of context-based arithmetic  
 106 encoders, they are included in some remote sensing coding  
 107 approaches [6], [19], [20]. Contributions aimed to reduce  
 108 the computational load by estimating the probability using  
 109 multiplication-free implementations can be found in the liter-  
 110 ature: the Q coder [21] approached the interval division  
 111 by means of lookup tables and the M coder [22] uses a  
 112 reduced range of possible subinterval sizes together with  
 113 lookup tables. Some methods based on these approaches  
 114 have been introduced in different standards [23]–[26]. The  
 115 operations carried out by the renormalization procedure can  
 116 be avoided if, instead of producing a single codeword, the  
 117 coder produces short codewords of fixed length [27], [28].  
 118 In particular, [28] presents a context-adaptive binary arithmetic  
 119 coder with fixed-length coderwords (FLWs) that outperforms  
 120 the MQ [29] and M coders in terms of coding performance.  
 121 FLW avoids the renormalization procedure but still estimates  
 122 probabilities through the division.

123 It is worth noting that none of the previously mentioned  
 124 contributions is devised to reduce the computation related to  
 125 probability estimation and the renormalization simultaneously.  
 126 In this paper, we propose an arithmetic encoder that: 1) utilizes  
 127 inexpensive operations to estimate probabilities; 2) does not  
 128 incorporate the renormalization procedure; and 3) employs a  
 129 simple context model. It yields strong coding performance at  
 130 low and high rates for remote sensing images. Our probability  
 131 estimation procedure builds on that of FLW. Originally, FLW  
 132 uses a sliding window to estimate the probability of the  
 133 symbols coded using a division operation. Herein, the sliding  
 134 window size of FLW is adapted to deal only with power of  
 135 two sizes, which allows the use of low-complexity bitwise  
 136 operations and spares the division.



Fig. 1. CCSDS-123 encoding scheme.

137 The proposed arithmetic coder is incorporated in a lossless  
 138 and near-lossless coding scheme, providing improved com-  
 139 pression performance over current remote sensing image com-  
 140 pression techniques. Roughly described, the adopted coding  
 141 scheme departs from the predictor and mapping included in  
 142 CCSDS-123 and utilizes a near-lossless quantizer, employs a  
 143 binary arithmetic coder that operates on a line-by-line and  
 144 bitplane-by-bitplane basis, introduces a new context model that  
 145 evaluates (at most) only causal adjacent samples, and uses only  
 146 bitwise operations to estimate symbol probabilities. Extensive  
 147 experimental results indicate that our proposed approach  
 148 improves on CCSDS-123 in terms of lossless compression  
 149 ratios and also outperforms a near-lossless version of the  
 150 sample-adaptive and block-adaptive coders of CCSDS-123,  
 151 JPEG-LS [30] and M-CALIC [6] in terms of lossless and near-  
 152 lossless coding performances. Comparing only the entropy  
 153 encoders, FLW is slightly better than MQ and interleaved  
 154 entropy coder (IEC) [31].

155 The rest of this paper is structured as follows. Section II  
 156 briefly reviews the CCSDS-123 coding system and a near-  
 157 lossless technique for coding systems based on prediction.  
 158 Section III describes our proposed context-based arithmetic  
 159 coder with bitwise probability estimation. Section IV describes  
 160 how our proposed arithmetic coder is incorporated in a coding  
 161 scheme that uses the predictor of CCSDS-123. Section V  
 162 presents the experimental results. Section VI concludes this  
 163 paper.

## 164 II. CCSDS-123 AND NEAR-LOSSLESS COMPRESSION

### 165 A. CCSDS-123

166 The CCSDS-123 standard, which is limited to encoding  
 167 samples of  $N = 16$  b/pixel/band, can be structured in three  
 168 stages: *predictor*, *mapper*, and *entropy encoder*. Fig. 1 illus-  
 169 trates the encoding pipeline of CCSDS-123.

170 In summary, the predictor estimates the value of the current  
 171 sample  $x_{i,j,k}$  using previously scanned samples. This predicted  
 172 sample is denoted by  $\tilde{x}_{i,j,k}$ . The prediction error  $\Lambda$  is com-  
 173 puted as

$$174 \Lambda_{i,j,k} = x_{i,j,k} - \tilde{x}_{i,j,k} \quad (2)$$

175 and then mapped to a non-negative integer  $\lambda_{i,j,k}$  called the  
 176 mapped prediction residual. The entropy encoder is in charge  
 177 of encoding  $\lambda_{i,j,k}$  without loss. For the entropy encoder in  
 178 CCSDS-123, one can choose between a sample- and a block-  
 179 adaptive encoder.

180 Further details of the CCSDS-123 stages can be found  
 181 in [12] and [32].

### 182 B. Near-Lossless Compression

183 For the encoder described above, the decoder can reproduce  
 184  $x_{i,j,k}$ , without loss. In this section, we discuss the addition of a

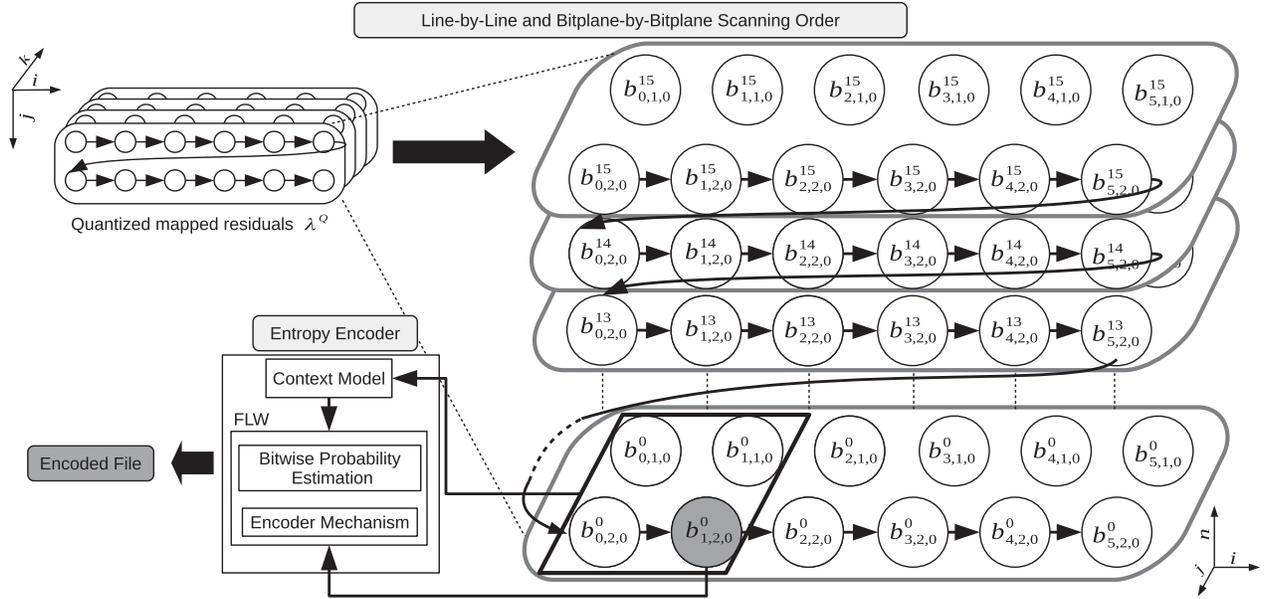


Fig. 2. Illustration of the scanning order and the entropy encoder.

185 quantizer, which results in higher compression ratios, but at the  
 186 expense of some loss of fidelity in the decompressed image.  
 187 The simplest and most effective way to design a  
 188 prediction-based lossy compression algorithm is to quantize  
 189 the prediction error  $\Lambda_{i,j,k}$  with a quantizer  $Q$ , resulting  
 190 in quantized-then-dequantized version  $\hat{\Lambda}_{i,j,k}$  (and, in conse-  
 191 quence,  $\hat{\lambda}_{i,j,k}$ ). The resulting quantization index is referred  
 192 to as  $\Lambda_{i,j,k}^Q$  and its remapped version is denoted by  $\lambda_{i,j,k}^Q$ .  
 193 Subsequent predictions  $\tilde{x}_{i,j,k}$  are calculated using previous  
 194 reconstructed (lossy) samples  $\hat{x}_{i,j,k}$ , which are obtained by  
 195 implementing a decoder in the encoder [12], [33]. The decoder  
 196 creates the reconstructed (lossy) image samples via

$$\hat{x}_{i,j,k} = \hat{\Lambda}_{i,j,k} + \tilde{x}_{i,j,k}. \quad (3)$$

198 It is worth noting that the errors in the reconstructed pixels  
 199 are identical to the errors introduced in the prediction errors  
 200 by the quantizer. That is,  $x_{i,j,k} - \hat{x}_{i,j,k} = \Lambda_{i,j,k} - \hat{\Lambda}_{i,j,k}$ . Thus,  
 201 the errors in reconstructed pixels can be precisely controlled  
 202 by controlling the individual quantization errors. This is the  
 203 basis of “near-lossless compression.”

### 204 III. LIGHTWEIGHT BINARY ARITHMETIC CODER 205 WITH CONTEXT MODEL

206 The entropy encoder presented in this paper works with  
 207 binary symbols. To this end, we denote the  $n$ th bit of the  
 208 binary representation of  $\lambda_{i,j,k}^Q$  by  $b_{i,j,k}^n$ , with  $N-1 \geq n \geq 0$ .  
 209 Here,  $N$  is chosen to provide a sufficient number of bits to  
 210 represent all the  $\lambda_{i,j,k}^Q$ , being  $b_{i,j,k}^{N-1}$  the most significant bit.

211 To facilitate use with on-board sensors, our proposal  
 212 processes data in a line-by-line fashion. Once a line is scanned,  
 213 predicted, and mapped to positive values, it is entropy encoded  
 214 on a bitplane-by-bitplane basis. The entropy encoder makes  
 215 use of context model patterns obtained using a context window  
 216 that contains symbols coded previously to the current symbol.

217 The top left of Fig. 2 displays the quantized and remapped  
 218 prediction residuals  $\lambda^Q$ . The binary representation of these  
 219 samples is shown on the right, while the bottom left portrays  
 220 the entropy encoder, which is fed by the current bit to be  
 221 encoded and its context. The bit to be encoded is shaded in  
 222 blue, while the context window is framed with a rectangle.

#### 223 A. Context Model

224 Let  $\mathbf{M}$  be the set of all possible patterns that can occur  
 225 within the context window, with context  $m \in \mathbf{M}$  being a  
 226 particular realization, resulting in a context index  $c \in \mathbf{C} =$   
 227  $\{0, \dots, C-1\}$ . These context indices (loosely referred to  
 228 as contexts in what follows) are determined by a modeling  
 229 function  $F: \mathbf{M} \rightarrow \mathbf{C}$ . For each bit  $b$  to be coded, a probability  
 230 model is used, corresponding to its context  $c$ . In particular,  
 231 the probability model estimates the conditional probability  
 232  $p(b|c) = p(b|F(m))$ . After encoding, the probability model is  
 233 updated with the latest coded bit  $b$ . That is,  $p(b|c)$  is estimated  
 234 on the fly. Specifically, our probability model estimates the  
 235 probability  $p(b=0|c)$ . A careful design of the context  
 236 model is required to obtain high coding efficiency. This task is  
 237 complicated by the goal of achieving low encoder complexity  
 238 for the purpose of operating on onboard remote sensing  
 239 scenarios.

240 A simple strategy for context modeling employs a context  
 241 window that contains only the three nearest causal neighbors  
 242 as depicted in Fig. 2. We consider several choices for the  
 243 context modeling function  $F$ . The first ignores all samples  
 244 within the context window except the one directly above the  
 245 sample of interest. This is indicated in Fig. 3(a). Three other  
 246 choices are shown in Fig. 3(b)–(d). The notations V, H, HV,  
 247 and HVD are used in Fig. 3, where V (vertical) denotes the  
 248 sample above the bit to be encoded, H (horizontal) denotes  
 249 the sample to the left, and D (diagonal) denotes the sample to

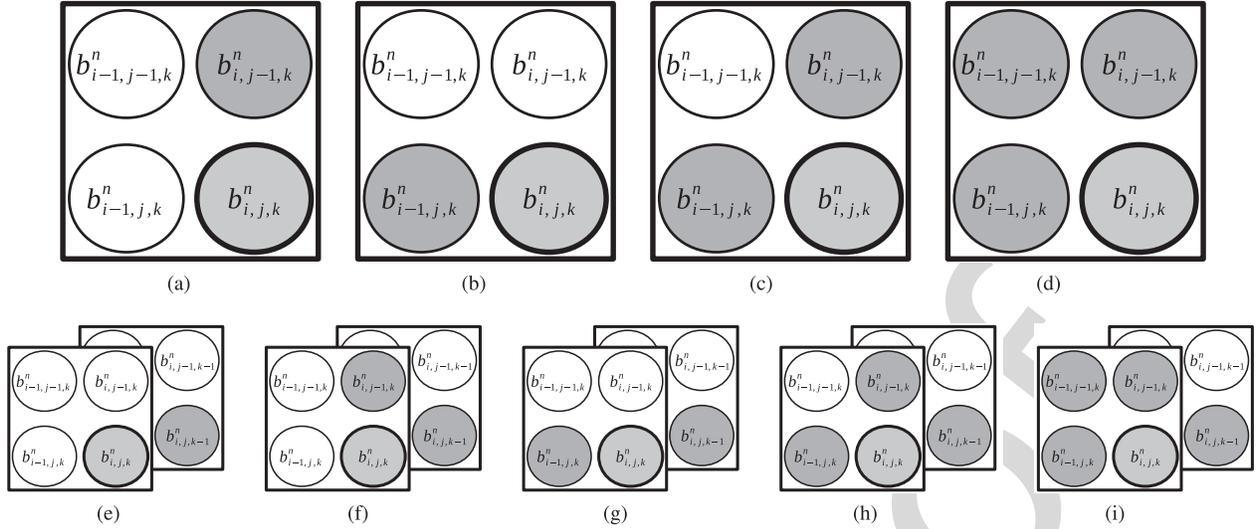


Fig. 3. Illustration of different context models to encode  $b_{i,j,k}^n$ . (a) V. (b) H. (c) HV. (d) HVD. (e) S. (f) VS. (g) HS. (h) HVS. (i) HVDS.

TABLE I  
CONTEXT ASSIGNMENTS FOR THE V, H, HV, AND HVD MODELING FUNCTIONS

$c$	V	H	HV		HVD		
	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i,j-1,k}^n$	$s_{i-1,j,k}^n$	$s_{i-1,j-1,k}^n$
0	0	0	0	0	0	0	0
1	1	1	0	1	0	0	1
2			1	0	0	1	0
3			1	1	0	1	1
4					1	0	0
5					1	0	1
6					1	1	0
7					1	1	1

the left and above. To take advantage of dependencies between spectral components, the preceding spectral component  $k - 1$  can be included in the context window. In this case, S (spectral) denotes the coregistered sample in the previous spectral component. The inclusion of this sample gives rise to five additional modeling functions as shown in Fig. 3(e)–(i). Note that if only samples H and S are employed by the modeling function, only the current scanned line must be stored in memory. For all other modeling functions, the previous and the current lines are necessary.

Rather than the actual bit (from bitplane  $n$ ) of each neighboring sample, the so-called “significance state” is employed to compute the context  $c$ . To this end, let  $s_{i,j,k}^n$  denote the significance state of the sample at location  $i, j, k$  at bitplane  $n$ . A value of 1 indicates that the sample contains a 1 at bitplane  $n$  or higher. Table I shows how  $c$  is derived from the significance states of the neighbors for the V, H, HV, and HVD modeling functions. The S modeling function results in two states, i.e.,  $c \in \{0, 1\}$ . The VS, HS, HVS, and HVDS modeling functions result in twice the number of states than their counterparts that do not employ S. They are not shown in Table I for the sake of space. The experimental results for all context modeling functions are presented in a subsequent section.

Before finishing this section, we note that the entropy coder and its associated probability models are initialized at the

beginning of each bit plane of each component. In particular, the initial probability model for each context is set to a value of  $p(b = 0|c) = 0.66$ . The probability is biased toward 0 since, as found empirically, bits of higher bitplanes have higher probability of being 0, thus allowing FLW to adapt faster. This, together with the fact that all bitplane data from the current line (and its predecessor, when relevant) are available in the encoder, leads to the conclusion that the bitplanes of the current line can be encoded in parallel. This parallel strategy is not possible in the decoder. The use of significant states in the context formation process requires that bitplanes be decoded sequentially. We note that the probabilities are reset ( $p(b = 0|c) = 0.66$ ) at the beginning of each component without penalizing the coding performance. This is because only  $2^{12}$  symbols are encoded with the default probability value, which on average for the image corpora used, corresponds to the 0.06% of the total symbols per band to be encoded.

### B. Bitwise Probability Estimation

As mentioned before, FLW was devised to reduce computational costs through the use of FLWs, which avoids a renormalization operation, but is not aimed to reduce the computational load derived from probability estimation [28].

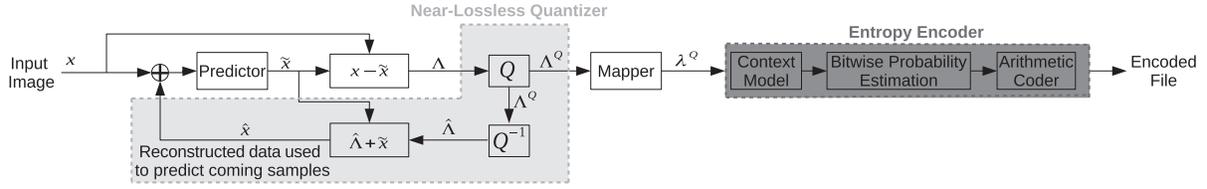


Fig. 4. Adopted coding approach.

 TABLE II  
 MAIN DIFFERENCES BETWEEN CCSDS-123 AND THE ADOPTED APPROACH

	Predictor	Quantizer	Mapper	Data Scanned	Supported	Context Model	Entropy Encoder
CCSDS-123	✓	✗	✓	Line or Block		✗	Sample-Adaptive or Block-Adaptive
Proposal	✓	✓	✓	Line		✓	Contextual Binary Arithmetic Coder

For each context  $c$ , FLW uses a sliding window of symbols coded with that context. The length of this window varies between  $\mathcal{T}$  and  $2\mathcal{T} - 1$  symbols. The probability estimate is updated once every  $\mathcal{V}$  symbols coded, according to

$$p(b = 0|c) = \frac{Z \ll \mathcal{B}}{W} \quad (4)$$

with  $W$  representing the number of symbols within the window,  $Z$  the number of zeroes within the window, and  $\mathcal{B}$  the number of bits used to express symbol probabilities. The numerator of the expression is computed by left shifting the binary representation of  $Z$  by  $\mathcal{B}$  bits. The size of the window is incremented each time a symbol is encoded using context  $c$  until  $W = 2\mathcal{T}$ , at which time the window size is immediately reduced to  $\mathcal{T}$  and the number of zeroes within the window is updated according to  $Z \leftarrow Z - Z'$  and  $Z' \leftarrow Z$ , with  $Z'$  being the number of zeroes coded during the most recent  $\mathcal{T}$  symbols.

In the original approach of FLW as formulated above,  $p(b|c)$  is computed via a division operation to achieve maximum accuracy. Such a division may tax the on-board computational resources in a remote sensing scenario. To reduce computational complexity, we propose to estimate the probability through bitwise operations. The substitution of the division by bitwise operations requires that  $\mathcal{V} = \mathcal{T}$  and that both are a power of two. This forces the sliding window to contain a power of two symbols, so the probability can be updated using only bit shift operations according to

$$p(b|c) = (Z \ll \mathcal{B}) \gg \log_2(W) \quad (5)$$

where  $W$  and  $Z$  are then updated through  $W \leftarrow W \gg 1$  and  $Z \leftarrow Z \gg 1$ . Note that this update rule for  $Z$  approximates only the number of zeroes in the most recent  $\mathcal{T}$  coded samples. Nevertheless, the update can be carried out in the decoder using the same approximation. At the beginning of encoding, the probability is first updated when  $\mathcal{V}$  symbols are coded. Subsequently, it is updated every  $\mathcal{V}/2$  symbols. The strategy proposed here can be seen as a special case of (4), which was not explored in [28].

Using (5) instead of (4) reduces the flexibility of the arithmetic coder since the updating of the probability estimates and the window size are tied together. The maximum performance

achieved with the original formulation of the arithmetic coder proposed in [28] is achieved when the probability estimate is updated every symbol, i.e.,  $\mathcal{V} = 1$ , regardless of the window size. The strategy proposed here provides a significant reduction in complexity with a minor reduction in compression performance. The experimental results provided in Section V indicate that our approach yields highly competitive compression performance.

#### IV. ADOPTED CODING APPROACH

Although the novel entropy encoder presented here may be incorporated in any coding system, we employ it in the CCSDS-123 coding pipeline. Fig. 4 illustrates the adopted coding approach, which employs the predictor and mapper of CCSDS-123, but adds a near-lossless quantizer (see the yellow block), and substitutes the usual CCSDS-123 encoder by our entropy encoder (see the green block). The circle containing a cross at the left side of Fig. 4 indicates that the input to the predictor is either the original pixel  $x$  (when the optional quantization is not present) or the reconstructed pixel  $\hat{x}$  (when quantization is present).

The adopted coding scheme is evaluated with a uniform quantizer (UQ) and a uniform scalar deadzone quantizer (USDQ) [29]. The UQ operates over  $\Lambda_{i,j,k}$  to obtain a quantization index according to

$$\Lambda_{i,j,k}^Q = \text{sign}(\Lambda_{i,j,k}) \left\lfloor \frac{|\Lambda_{i,j,k}| + \Delta}{2\Delta + 1} \right\rfloor \quad (6)$$

where  $2\Delta + 1$  is the quantization step size. The operation to reconstruct  $\hat{\Lambda}_{i,j,k}$  from its quantization index is given by

$$\hat{\Lambda}_{i,j,k} = \text{sign}(\Lambda_{i,j,k}^Q) (2\Delta + 1) \Lambda_{i,j,k}^Q. \quad (7)$$

The UQ is employed in lossless compression techniques such as JPEG-LS, M-CALIC, and 3-D-CALIC [34]. On the other hand, the USDQ quantizes  $\Lambda_{i,j,k}$  to obtain a quantization index according to

$$\Lambda_{i,j,k}^Q = \text{sign}(\Lambda_{i,j,k}) \left\lfloor \frac{|\Lambda_{i,j,k}|}{\Delta + 1} \right\rfloor \quad (8)$$

TABLE III

SUMMARY OF DATA USED IN THE EXPERIMENTAL RESULTS. SENSOR NAME, ITS ABBREVIATION, THE NUMBER OF IMAGES FROM EACH SENSOR, AND FIRST-ORDER ENTROPIES (IN BITS PER SAMPLE) ON AVERAGE PER SENSOR ARE PROVIDED. THE LAST TWO COLUMNS INDICATE THE PREDICTOR MODE AND THE LOCAL SUM USED FOR EACH SENSOR

Sensor	Abbreviation	Number of images	Entropy	Predictor Mode	Local Sum
Aviris Calibrated	AC	5	9.77	Neighbor Oriented	Full Mode
Aviris Uncalibrated	AU	7	11.21	Neighbor Oriented	Full Mode
Airs	A	9	11.34	Neighbor Oriented	Reduced Mode
Casi	C	2	10.52	Neighbor Oriented	Reduced Mode
Crism	Cr	20	10.69	Column Oriented	Reduced Mode
Hyperion	H	4	9.53	Column Oriented	Reduced Mode
M3	M3	5	9.19	Column Oriented	Reduced Mode
Total / average	—	52	10.41	—	—

371 where the quantization step is  $\Delta + 1$ . The operation to  
372 reconstruct  $\hat{\Lambda}_{i,j,k}$  from its quantization index is expressed as

$$373 \quad \hat{\Lambda}_{i,j,k} = \text{sign}(\Lambda_{i,j,k}^Q)(\Delta + 1)\Lambda_{i,j,k}^Q. \quad (9)$$

374 Due to its straightforward implementation and excellent  
375 performance, the USDQ has been selected for the JPEG  
376 2000 standard [24]. The USDQ partitions the range of input  
377 values into intervals all of size  $\Delta$ , except for the interval that  
378 contains zero, which is of size  $2\Delta$ . This results in all absolute  
379 pixel errors  $|x_{i,j,k} - \hat{x}_{i,j,k}|$  being bounded above  $\Delta$  for both  
380 quantizers.

381 Table II summarizes the main differences between  
382 CCSDS-123 and the adopted coding scheme.

## 383 V. EXPERIMENTAL RESULTS

384 This section presents a set of experiments aimed at the  
385 analysis and evaluation of the adopted coding scheme. First,  
386 the proposed context modeling functions are evaluated in  
387 terms of the conditional entropy of the prediction residual.  
388 The bitwise probability estimator is then evaluated via the  
389 same performance metric to determine its proper configuration.  
390 A variety of binary encoder mechanisms such as IEC, MQ,  
391 and FLW are evaluated in terms of their lossless compression  
392 performance in conjunction with the proposed context  
393 modeling and probability estimation. Finally, the resulting  
394 proposed overall approach is compared in terms of lossless and  
395 near-lossless compression performances with CCSDS-123,  
396 JPEG-LS, and M-CALIC.

397 For the experiments conducted in this paper, we have  
398 selected a set of images<sup>1</sup> collected with different sensors that  
399 are included in CCSDS MHDC-WG corpus. The sensor names  
400 and their main features are listed in Table III. The average  
401 entropy is reported for each image type. The reported values  
402 are first-order entropy; they represent the entropy of individual  
403 pixels, without accounting for any dependencies among pixels  
404 within or between components.

405 In [35], the impact of different CCSDS-123 parameters  
406 that control the operation of the prediction and the entropy  
407 encoder was evaluated, suggesting that a correct parameter

408 selection had more impact on the predictor stage than in  
409 the entropy encoder stage. Concerning the prediction, the  
410 parameters local sum type, prediction mode, the number of  
411 prediction bands, and predictor adaption rate were the most  
412 critical. Extensive experimental evaluations were conducted to  
413 find suitable configurations.

414 In this paper, leaning on the results in [35] and after  
415 conducting an extensive evaluation also, experimental results  
416 are produced for the following parameter configuration: the  
417 local sum type and predictor mode depend on the acquisition  
418 sensor (as indicated in the last two columns of Table III);  
419 the number of prediction bands  $P$  is set to 3, since it is a  
420 good tradeoff between the computational load and the coding  
421 performance; and the predictor adaptation rate  $v_{\max}$  is set to 3,  
422 since, in general, it yields the best performance.

423 For evaluating the performance of context modeling and  
424 probability estimation, we employ the conditional entropy of  
425 the prediction residuals, as mentioned above. For the work  
426 proposed here, binary entropy coding is employed. To yield  
427 results with units in bits per pixel, the binary entropies of  
428 all bitplanes are added. Since our context model estimates the  
429 probability of  $p(b = 0|c)$ , the conditional entropy of an image  
430 (in bits) is computed as

$$431 \quad H(\lambda^Q) = \sum_{i=0}^{I-1} \sum_{j=0}^{J-1} \sum_{k=0}^{K-1} \sum_{n=0}^{15} \quad (10)$$

$$432 \quad \times \begin{cases} \log_2(p(b_{i,j,k}^n = 0|c)) & \text{if } b_{i,j,k}^n = 0 \\ \log_2(1 - p(b_{i,j,k}^n = 0|c)) & \text{if } b_{i,j,k}^n = 1 \end{cases}$$

433 where  $\lambda^Q$  denotes the symbols to be entropy coded.

### 434 A. Context Modeling Function

435 The context model is used to select the probability model  
436 that is employed to encode the current symbol. In this first  
437 experiment, each of the probability models themselves is  
438 estimated using the high-performance method given by (4)  
439 employing  $\mathcal{V} = 1$  and  $\mathcal{T} = 2^{12}$ , without regard to complexity.

440 Table IV provides the conditional entropy obtained (in bits  
441 per sample) for the different context formations defined in  
442 Section III-A, i.e., V, H, HV, HVD, S, VS, HS, HVS, and  
443 HVDS. The results from Table III suggest the following.

<sup>1</sup>The images used are available at <http://cwe.ccsds.org/sls/docs/sls-dc/123.0-B-Info/TestData>

TABLE IV

CONDITIONAL ENTROPY OF THE PREDICTION RESIDUALS (IN BITS PER SAMPLE) FOR THE CONTEXT MODELING FUNCTIONS DENOTED BY V, H, HV, HVD, S, VS, HS, HVS, AND HVDS. RESULTS ARE REPORTED ON AVERAGE FOR DIFFERENT SENSORS AND  $\Delta = 0$

Sensor	Context Formation								
	V	H	HV	HVD	S	VS	HS	HVS	HVDS
AC	3.69	3.69	3.68	3.68	3.69	3.68	3.68	3.68	3.67
AU	5.01	5.00	5.00	4.99	5.00	4.99	4.99	4.99	4.99
A	4.24	4.23	4.24	4.24	4.24	4.24	4.24	4.24	4.23
C	4.85	4.85	4.84	4.84	4.85	4.84	4.84	4.83	4.83
Cr	4.15	4.21	4.14	4.14	4.20	4.12	4.19	4.12	4.12
H	4.26	4.26	4.25	4.25	4.29	4.26	4.26	4.25	4.25
M3	2.66	2.70	2.65	2.65	2.70	2.64	2.68	2.63	2.63
Average	4.12	4.14	4.11	4.11	4.14	4.11	4.13	4.10	4.10

TABLE V

CONDITIONAL ENTROPY OF THE PREDICTION RESIDUALS (IN BITS PER SAMPLE) FOR  $\Delta = 0$  RESULTING FROM THE MAXIMUM PRECISION AND THE BITWISE PROBABILITY ESTIMATORS. THE V CONTEXT MODEL IS EMPLOYED IN EACH CASE. THE BEST RESULTS FOR EACH STRATEGY ARE REPRESENTED IN BOLD

$\mathcal{T} =$	division $\mathcal{V} = 1$					bitwise operations $\mathcal{V} = \mathcal{T}$				
	$2^{16}$	$2^{14}$	$2^{12}$	$2^{10}$	$2^8$	$2^{16}$	$2^{14}$	$2^{12}$	$2^{10}$	$2^8$
	AC	3.70	3.69	<b>3.69</b>	3.70	3.75	3.72	3.70	<b>3.69</b>	3.70
AU	5.02	5.01	<b>5.01</b>	5.01	5.06	5.04	5.02	<b>5.01</b>	5.02	5.08
A	4.27	4.26	<b>4.23</b>	4.24	4.26	4.32	4.29	<b>4.24</b>	4.26	4.28
C	4.94	4.86	<b>4.85</b>	4.86	4.89	4.90	4.86	<b>4.85</b>	4.86	4.91
Cr	4.16	4.15	<b>4.15</b>	4.15	4.18	4.21	4.17	<b>4.16</b>	4.16	4.20
H	4.27	4.26	<b>4.26</b>	4.27	4.31	4.29	4.27	<b>4.26</b>	4.27	4.32
M3	2.69	2.66	<b>2.66</b>	2.67	2.70	2.71	2.68	<b>2.67</b>	2.68	2.72
Average	4.15	4.13	<b>4.12</b>	4.13	4.16	4.17	4.14	<b>4.13</b>	4.13	4.18

- 1) All of the modeling functions provide significant improvements over the pixel entropy reported in Table III.
  - 2) The differences in performance between the modeling functions are generally small.
  - 3) Although the context models H and S yield the worst performance on average, they are the best option when memory resources are severely limited since they need only to store samples from the current line to be encoded.
  - 4) Adding the S sample to a context results in an improvement of only about 0.01 b/sample.
  - 5) The V context obtains a coding benefit of 0.02 b/sample on average with respect to the H context and only adds the previous processed line to its storage requirements.
- In what follows, we select context model V for further evaluation due to its favorable tradeoff among the performance, memory resources, and computational load.

estimation strategies. In both cases, the V context model is employed. The left of Table V presents results for the maximum precision technique (using division), as defined by (4). These results are shown for different values of  $\mathcal{T}$ , but  $\mathcal{V} = 1$ . The right side of Table V presents results for the bitwise strategy, as defined by (5). The same values of  $\mathcal{T}$  are explored, but always with  $\mathcal{V} = \mathcal{T}$ , as required to avoid division. The results suggest that  $\mathcal{T} = 2^{12}$  attains the highest performance for both strategies. A larger  $\mathcal{T}$  degrades the coding performance because the window may contain symbols that are not correlated with the current one. A smaller  $\mathcal{T}$  degrades the coding performance because there are insufficient symbols to reliably estimate the probabilities  $p(b|C)$ . The results of Table V also indicate that the low-complexity strategy that employs bitwise operations is as competitive as that employing division. Although not tabulated here for the sake of space, these results hold for the other context modeling functions considered in the previous sections.

*B. Probability Estimation*

This section reports the results obtained by the two different probability estimation strategies discussed in Section III. In particular, Table V reports the conditional entropy of the prediction residuals resulting from the two different probability

*C. Entropy Coding*

We note that the context model and probability estimator proposed here can be used with any entropy encoder that codes binary symbols according to a given probability model, such as MQ, IEC or the adopted FLW. Table VI provides the actual

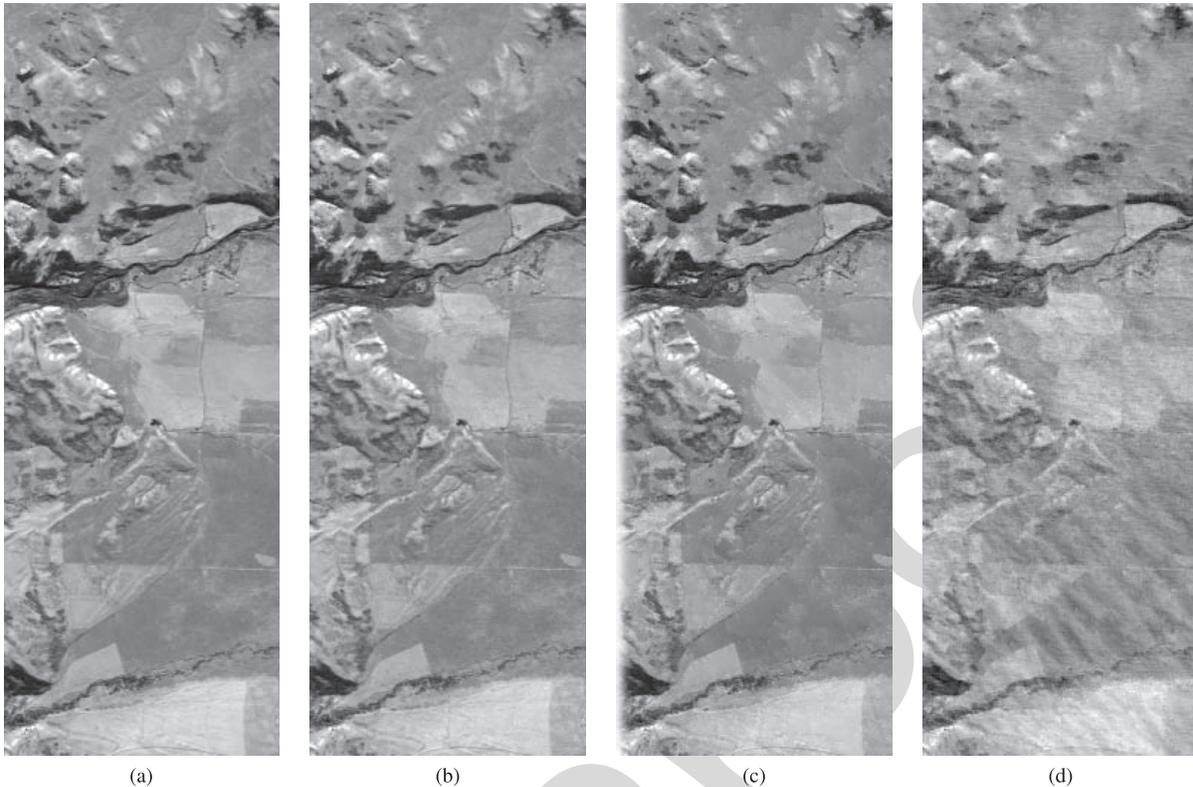


Fig. 5. Visual comparison for the “Avisis Calibrated Yellowstone sc00” image. (a) Original. (b) Proposed approach at 0.43 b/sample ( $\Delta = 20$ ). (c) M-CALIC at 0.42 b/sample ( $\Delta = 30$ ). (d) CCSDS-123 at 0.50 b/sample ( $\Delta = 80$ ).

TABLE VI  
CODING PERFORMANCE (IN Bits per Sample) OF THE PROPOSED  
APPROACH USING MQ, IEC, AND FLW ENTROPY ENCODING.  
ALL RESULTS EMPLOY CONTEXT MODEL V AND BITWISE  
PROBABILITY ESTIMATION WITH  $T = \mathcal{V} = 2^{12}$

Sensor	MQ	IEC	FLW
AC	3.74	3.72	3.71
AU	5.06	5.04	5.03
A	4.30	4.29	4.28
C	4.90	4.88	4.87
Cr	4.20	4.18	4.18
H	4.31	4.29	4.28
M3	2.71	2.70	2.69
Average	4.17	4.16	4.15

490 compression results (in bits per sample) obtained using the  
491 MQ, IEC, and FLW entropy coders. In each case, the results  
492 are obtained with context model V and the bitwise estimator  
493 with  $T = \mathcal{V} = 2^{12}$ . From these results, we can see that, on  
494 average, FLW yields slightly better results than IEC and MQ.

#### 495 D. Lossless and Near-Lossless Compression

496 The results reported in this section compare the loss-  
497 less performance of the proposed approach with those of  
498 JPEG-LS, M-CALIC, and CCSDS-123. Additionally, we com-  
499 pare its *near-lossless* performance with those of JPEG-LS  
500 and M-CALIC and the implementation of CCSDS-123.  
501 Different quantizers have been combined with our proposal  
502 and CCSDS-123, to obtain an as fair as possible comparison.

In particular, the UQ and the USDQ discussed in Section IV  
are compared.

M-CALIC and the near-lossless version of CCSDS-123 are  
considered to be state of the art in terms of compression  
performance and computational complexity, and JPEG-LS is a  
standard technique with near-lossless features. All results for  
the proposed scheme are produced using the FLW arithmetic  
coder, context model V, and the bitwise probability estimator  
having  $\mathcal{V} = T = 2^{12}$ . The results reported in Table VII  
indicate that our method outperforms both M-CALIC and  
CCSDS-123 in terms of lossless coding ( $\Delta = 0$ ) for all  
sensors. In the near-lossless regime ( $\Delta > 0$ ), the proposed  
approach outperforms M-CALIC when the USDQ is used and  
in most cases for the UQ. In particular, M-CALIC obtains  
slightly better results than our proposal only for images  
acquired with sensors AIRS and Hyperion when the UQ  
is used. On the other hand, the proposed system always  
outperforms the near-lossless extension of CCSDS-123 for  
both quantizers. In addition, in general, for the same  $\Delta$  value,  
the coding performance is better for the USDQ than for UQ.  
Although achieved bit rates vary widely from image to image,  
low bit rates can be obtained for all images with a modest  
value of PAEs (maximum absolute pixel error).

#### E. Visual Comparison

To evaluate visual performance, we show a region cropped  
from an image encoded at the “same” bit rate by the proposed  
approach with the UQ, M-CALIC, and CCSDS-123. For  
CCSDS-123, we employ the block-adaptive coder since we  
want to compare the images at a bit rate lower than 1 b/sample.

TABLE VII

LOSSLESS ( $\Delta = 0$ ) AND NEAR-LOSSLESS ( $\Delta > 0$ ) COMPRESSION RESULTS FOR THE PROPOSED APPROACH. FOR COMPARISON, THE RESULTS FOR JPEG-LS, M-CALIC, AND CCSDS-123 ARE INCLUDED. BOTH A UQ AND A USDQ HAVE BEEN USED IN OUR PROPOSED APPROACH AND IN OUR NEAR-LOSSLESS EXTENSION TO CCSDS-123 TO PRODUCE RESULTS FOR  $\Delta > 0$ . THE RESULTS ARE REPORTED IN BITS PER SAMPLE (LOWER IS BETTER)

Sensor	$\Delta$ values	CCSDS-123				JPEG-LS	M-CALIC	Our Proposal	
		with UQ		with USDQ				with UQ	with USDQ
		Sample adaptive	Block adaptive	Sample adaptive	Block adaptive				
AC	$\Delta = 0$	3.73	3.91	3.73	3.91	6.41	3.87	<b>3.71</b>	<b>3.71</b>
	$\Delta = 10$	1.20	0.97	1.20	0.94	2.45	0.76	<b>0.62</b>	<b>0.60</b>
	$\Delta = 20$	1.10	0.74	1.10	0.72	1.81	0.50	<b>0.38</b>	<b>0.36</b>
	$\Delta = 30$	1.07	0.64	1.07	0.63	1.48	0.40	<b>0.28</b>	<b>0.27</b>
AU	$\Delta = 0$	5.06	5.23	5.06	5.23	7.47	5.13	<b>5.03</b>	<b>5.03</b>
	$\Delta = 10$	1.69	1.68	1.85	1.78	3.41	1.46	<b>1.39</b>	1.52
	$\Delta = 20$	1.35	1.19	1.40	1.21	2.68	0.95	<b>0.87</b>	0.90
	$\Delta = 30$	1.24	0.98	1.26	0.99	2.30	0.73	<b>0.65</b>	0.67
A	$\Delta = 0$	4.29	4.48	4.29	4.48	6.85	4.28	<b>4.27</b>	<b>4.27</b>
	$\Delta = 10$	1.23	1.12	1.18	0.96	2.62	0.73	0.76	<b>0.62</b>
	$\Delta = 20$	1.10	0.75	1.07	0.65	1.86	0.41	0.39	<b>0.30</b>
	$\Delta = 30$	1.06	0.63	1.05	0.56	1.50	0.31	0.28	<b>0.22</b>
C	$\Delta = 0$	4.97	5.15	4.97	5.15	6.79	4.91	<b>4.87</b>	<b>4.87</b>
	$\Delta = 10$	1.47	1.48	1.51	1.47	2.64	1.12	<b>1.10</b>	<b>1.10</b>
	$\Delta = 20$	1.25	1.06	1.25	1.03	1.94	0.68	0.67	<b>0.64</b>
	$\Delta = 30$	1.17	0.88	1.18	0.87	1.58	0.52	0.49	<b>0.48</b>
Cr	$\Delta = 0$	4.40	4.50	4.40	4.50	5.10	6.91	<b>4.18</b>	<b>4.18</b>
	$\Delta = 10$	1.64	1.66	1.63	1.42	1.83	2.75	1.26	<b>0.99</b>
	$\Delta = 20$	1.43	1.34	1.39	1.05	1.47	2.02	0.92	<b>0.64</b>
	$\Delta = 30$	1.34	1.17	1.30	0.89	1.29	1.64	0.76	<b>0.50</b>
H	$\Delta = 0$	4.37	4.57	4.37	4.57	6.24	4.80	<b>4.28</b>	<b>4.28</b>
	$\Delta = 10$	1.38	1.45	1.21	1.08	2.74	1.02	1.06	<b>0.68</b>
	$\Delta = 20$	1.24	1.19	1.09	0.74	2.06	0.52	0.77	<b>0.35</b>
	$\Delta = 30$	1.18	1.04	1.06	0.63	1.68	0.33	0.62	<b>0.25</b>
M	$\Delta = 0$	2.81	2.97	2.81	2.97	4.24	5.18	<b>2.69</b>	<b>2.69</b>
	$\Delta = 10$	1.26	1.21	1.11	0.74	1.38	1.32	0.76	<b>0.33</b>
	$\Delta = 20$	1.17	1.01	1.07	0.60	1.20	0.78	0.56	<b>0.20</b>
	$\Delta = 30$	1.14	0.89	1.06	0.55	1.00	0.53	0.46	<b>0.15</b>
Average	$\Delta = 0$	4.23	4.40	4.23	4.40	6.16	5.01	<b>4.15</b>	<b>4.15</b>
	$\Delta = 10$	1.41	1.37	1.39	1.20	2.44	1.31	1.00	<b>0.83</b>
	$\Delta = 20$	1.23	1.04	1.20	0.86	1.86	0.84	0.65	<b>0.48</b>
	$\Delta = 30$	1.17	0.89	1.14	0.73	1.55	0.64	0.51	<b>0.36</b>

We note that none of the schemes compared here includes precise rate control. For this reason, we have employed the following methodology: 1) encode an image using a variety of different quantization step sizes for each compression scheme and 2) choose those encoded images that yield bit rates as close as possible for the three algorithms. We note that a close match was not obtained in the case of CCSDS-123, so a step size was chosen to afford a higher bit rate than that of the proposed approach, thus giving an advantage to CCSDS-123 in terms of visual performance.

The results of this process are shown in Fig. 5 for a crop from component 122 of the image “Avisis Calibrated Yellowstone sc00.” The bit rates obtained are 0.43, 0.42, and 0.50 for the proposed approach, M-CALIC, and CCSDS-123, respectively. The reader is invited to zoom in to see the specific visual artifacts arising from the different compression

schemes. Fig. 5 indicates that the image obtained by the proposed approach has higher visual quality than those by (near lossless) CCSDS-123 and M-CALIC. In particular, the proposed approach preserves edges and textures very well, while M-CALIC results in smoothness and loss of texture. CCSDS-123 also removes texture, but also introduces an annoying “banding” effect, due to the high step size required to reach 0.50 b/sample.

VI. CONCLUSION

This paper proposes an entropy encoder based on an efficient definition for a context model and the associated strategy to estimate probabilities for use in a fixed-length arithmetic encoder using low-cost bitwise operations. These contributions are incorporated in a coding approach that employs the predictor included in CCSDS-123. A near-lossless

quantizer has also been deployed. The entropy encoder works on a line-by-line and bitplane-by-bitplane scanning order. The experimental results indicate that the use of a single neighbor for the context formation is enough to properly exploit the contextual information in the arithmetic encoder and that it is possible to estimate the probability employing bitwise operations without penalizing the coding efficiency. Further results indicate that, on average, our proposal improves the current standard version of CCSDS-123 for lossless coding by more than 0.1 b/sample. Compared with M-CALIC, our proposal provides an average improvement of 0.86 b/sample for lossless, whereas for near-lossless, the benefit ranges from 0.13 to 0.31 b/sample, depending on the allowed PAE.

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