

PINFER: PRIVACY-PRESERVING INFERENCE

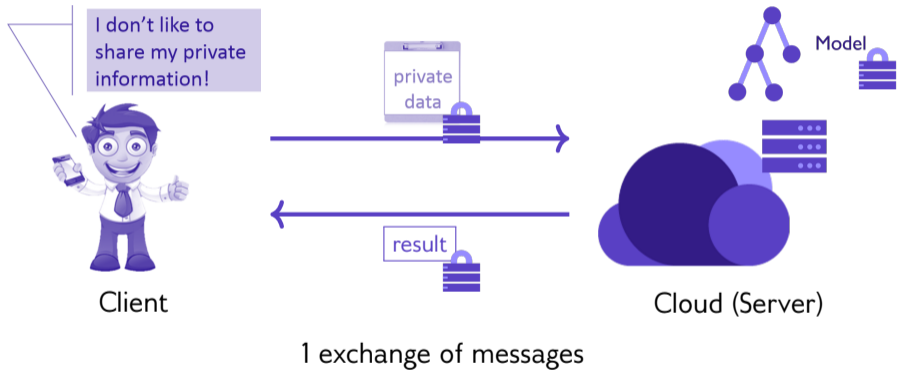
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MACHINE LEARNING AS A SERVICE — GENERIC MODEL



Security requirements



- The server learns nothing about the client's input
- The server does not learn the output of the calculation
- The client learns nothing about the ML model

Proposed solutions

Private evaluation for:

- 1 Linear regression
 - Support Vector Machines (SVM)
 - requires a private comparison protocol (e.g., DGK+)
- 2 Logistic regression
- 3 Binary classification
- 4 Neural networks
 - Sign or ReLU activation functions
 - 1 interaction per layer

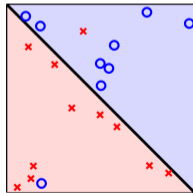
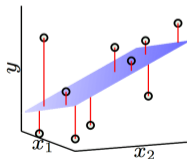
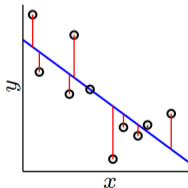
LINEAR PREDICTION MODEL

- Input

- 1 Server's ML model: $\theta = (\theta_0, \dots, \theta_d) \in \mathbb{R}^{d+1}$
- 2 User's feature vector: $\mathbf{x} = (1, x_1, \dots, x_d) \in \{1\} \times \mathbb{R}^d$

- Output

$$h_{\theta}(\mathbf{x}) = g(\theta^T \mathbf{x}) \quad \text{in many cases}$$

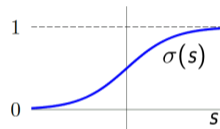


Linear Regression [real-valued output]

$$g = \text{Id}$$

Logistic Regression [probability]

$$g = \sigma \quad \text{where } \sigma(s) = \frac{\exp(s)}{1 + \exp(s)}$$



Linear Classification [binary decision]

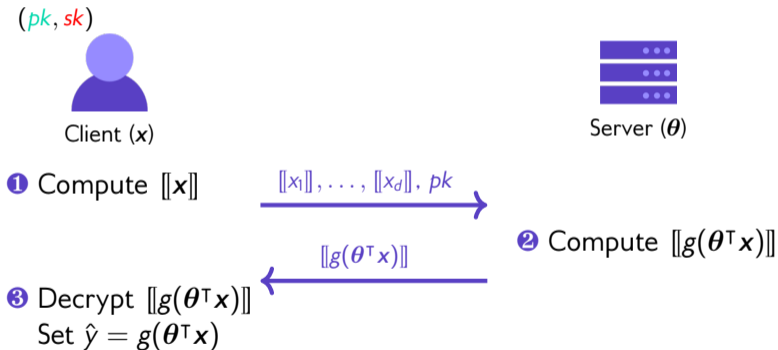
$$g = \text{sign}$$

Rectified linear unit (ReLU) [neural networks]

$$g(s) = \begin{cases} 0 & \text{if } s < 0 \\ s & \text{otherwise} \end{cases}$$

LINEAR PREDICTION MODEL WITH ENCRYPTION

$$\text{Model evaluation: } \hat{y} = g(\boldsymbol{\theta}^T \mathbf{x})$$



- We only require linearly homomorphic encryption:

$$\text{Enc}_{pk}(m_1) \boxplus \text{Enc}_{pk}(m_2) = \text{Enc}_{pk}(m_1 + m_2)$$

- **NOT** fully homomorphic encryption:

$$\text{Enc}_{pk}(m_1) \boxplus \text{Enc}_{pk}(m_2) = \text{Enc}_{pk}(m_1 + m_2)$$

$$\text{Enc}_{pk}(m_1) \boxdot \text{Enc}_{pk}(m_2) = \text{Enc}_{pk}(m_1 \cdot m_2)$$

- Benefits
 - Simpler implementation
 - Faster computation

- Since $[[\cdot]]$ is homomorphic

$$[[\boldsymbol{\theta}^T \mathbf{x}]] = [[\theta_0 + \sum_{i=1}^d \theta_i x_i]] = [[\theta_0]] \boxplus [[\theta_1 x_1]] \boxplus \cdots \boxplus [[\theta_d x_d]]$$

and, for $1 \leq i \leq d$,

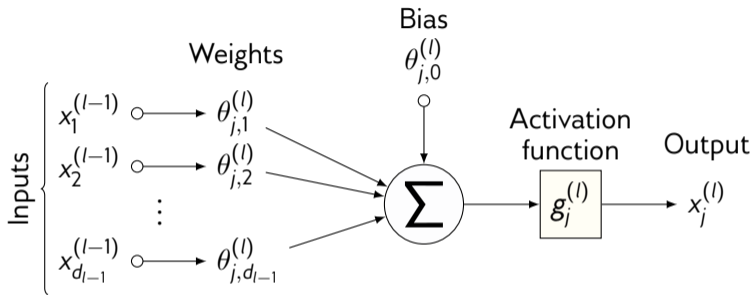
$$[[\theta_i x_i]] = \underbrace{[[x_i]] \boxplus \cdots \boxplus [[x_i]]}_{\theta_i \text{ times}} := \theta_i \odot [[x_i]]$$

Example (Paillier's cryptosystem)

- $[[m]] = (1 + N)^m r^N \bmod N^2$
- $[[m_1 + m_2]] = [[m_1]] \cdot [[m_2]] \bmod N^2$
- $[[m_1 - m_2]] = [[m_1]] / [[m_2]] \bmod N^2$
- $a \odot [[m]] = [[m]]^a \bmod N^2 \implies [[\boldsymbol{\theta}^T \mathbf{x}]]$ requires d exponentiations modulo N^2

IF EVALUATION FUNCTION g IS NON-LINEAR

- g is non-linear but injective (e.g., σ)
 - Server computes $\llbracket \theta^\top x \rrbracket$
 - Client obtains $\theta^\top x$ and simply applies g and learns no more (by definition: $g(a) = g(b) \implies a = b$)
- g is non-linear and non-injective (e.g., sign, ReLU)
 - Use set of tools and tricks
 - DGK+ comparison protocol
 - Simple masking with a random value
 - Masking and scaling of inner product
 - Variant of oblivious transfer (two possible ciphers sent)
 - Dual setup
 - Server publishes pk_s and $\llbracket \theta \rrbracket_s$
 - Still one round of messages!



- Implementation (not much optimised)
 - Python
 - Intel i7-4770, 3.4GHz
 - GMP library (power exponentiation)
 - Fixed precision (53 bits)
- Parameters
 - Public datasets and randomly generated ones
 - Models with 30 to 7994 features
 - Key sizes: 1388 to 2440 bits
- Message overhead proportional to:
 - Key size
 - Number of features (or number of bits in DGK+)
 - Number of layers (FFNN)

MESSAGE OVERHEAD

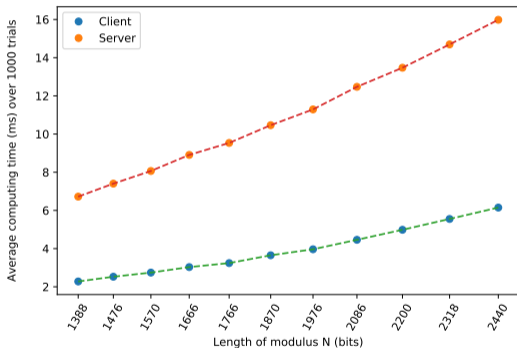
Protocol	Protocol step	Size	(kB) ¹
Linear regression (core)	Client sends: $pk_C, \llbracket x_i \rrbracket, 1 \leq i \leq d$	$l_M + d \cdot 2l_M$	≈ 15
	Server sends: t	$\approx 2l_M$	< 1
SVM classification (core)	Client sends $t^*, \llbracket \mu_i \rrbracket, 0 \leq i \leq \ell - 1$	$2l_M + \ell \cdot 2l_M$	≈ 29
	Server sends $\llbracket h_i^* \rrbracket, -1 \leq i \leq \ell - 1$	$(\ell + 1) \cdot 2l_M$	≈ 30
FFNN sign act. (core)	Server sends $t^*, \llbracket \mu_i \rrbracket_S, 0 \leq i \leq \ell - 1$	$L \cdot d \cdot (\ell + 1) \cdot 2l_M$	2,655 (885 per layer)
	Client sends $\llbracket \hat{y}^* \rrbracket, \llbracket h_i^* \rrbracket_S, -1 \leq i \leq \ell - 1$	$L \cdot d \cdot (\ell + 2) \cdot 2l_M$	2,700 (900 per layer)

¹Features: $d = 30$; key-size $l_M = 2048$; $\kappa = 95$; layers $L = 3$; Precision $P = 53$;
Inner-product bound: $\ell = 58$

RESULTS: LINEAR REGRESSION

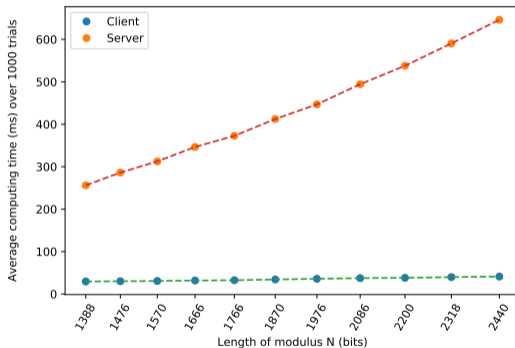
Private LR: 70 features

Private linear regression (core protocol)
Dataset: audiology, # features: 70



Private LR: 7994 features

Private linear regression (core protocol)
Dataset: enron, # features: 7994

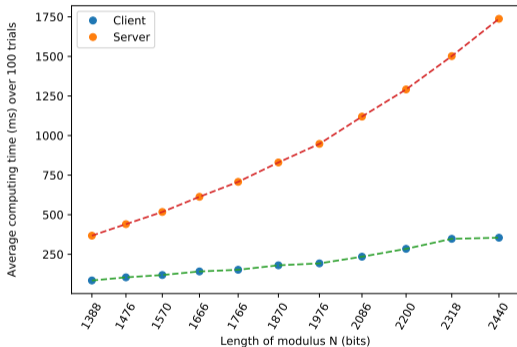


On Intel i7-4770, 3.4GHz

RESULTS: SUPPORT VECTOR MACHINE CLASSIFICATION

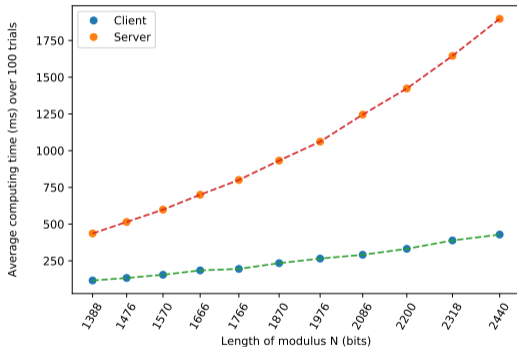
Private SVM: 70 features

Private SVM classification (core protocol)
Dataset: audiology, # features: 70



Private SVM: 7994 features

Private SVM classification (core protocol)
Dataset: enron, # features: 7994

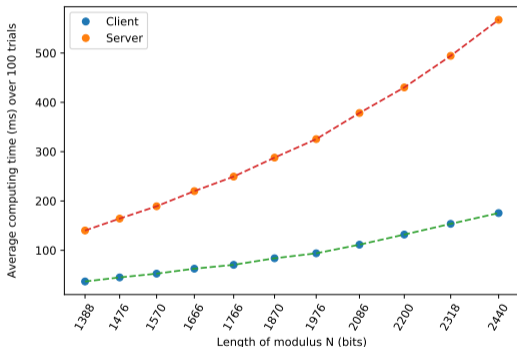


On Intel i7-4770, 3.4GHz

DGK+ comparison is the main limiting factor

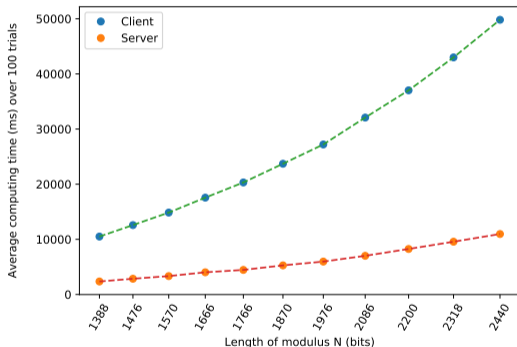
Private NNs: 10 features | 3 layers

simple FFNN with sign activation (heuristic solution)
Dataset: random, # features: 10, # layers: 3



Private NNs: 10 features | 3 layers

simple FFNN with sign activation
Dataset: random, # features: 10, # layers: 3



On Intel i7-4770, 3.4GHz

DGK+ comparison is the main limiting factor

