

# Anonymous and Transferable Electronic Ticketing Scheme

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# Introduction

- IT industry: smartphones revolution
  - Computation power
  - Storage capacity
  - Communication technologies (NFC, Wi-Fi, 4G, etc.)
  - Mobility+flexibility: payment and ticketing schemes
- Ticket: representation of the owner's rights to receive a determined service
  - At least, the same security requirements have to be fulfilled as in paper format
  - Requirements mainly depend on the service

# Contribution

- E-ticketing system
- Group signatures
- Security requirements:
  - Anonymity (revocable)
  - Short-term linkability (adaptation from BBS scheme)
  - Transferability
- Easily deployable to real scenarios

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# Security assumptions

## Definition (The $q$ -Strong Diffie-Hellman problem, SDH)

Given two cyclic groups  $G_1$  and  $G_2$  of prime order  $p$ , two randomly chosen generators  $g_1 \in G_1$  and  $g_2 \in G_2$  of their respective groups, with an isomorphism  $\psi : G_2 \rightarrow G_1$  where  $g_1 = \psi(g_2)$ , the  $q$ -SDH problem is a hard computational problem where the  $(q+2)$ -tuple

$(g_1, g_2, g_2^\gamma, g_2^{\gamma^2}, \dots, g_2^{\gamma^q}) \in G_1 \times G_2^{q+1}$  is the input and the pair

$(g_1^{\frac{1}{x+\gamma}}, x) \in G_1 \times \mathbb{Z}_p$  is the output, for some  $x \in \mathbb{Z}_p^*$  such that  $x + \gamma \neq 0$ .

## Definition (The Decision Linear Diffie-Hellman problem, DLIN)

Given a cyclic group  $G_1$  of order  $p$ , and taking  $u, v, h, u^a, v^b, h^c \in G_1$  as input, where  $u, v, h \in G_1$  randomly chosen generators, and random  $a, b, c \in \mathbb{Z}_p$ , and output *yes* if  $a + b = c$  and *no* otherwise.

# Procedures

- BBS scheme:
  - $KeyGen_G$
  - $Sign_G$
  - $Verify_G$
  - $Open_G$
- ZKP of the BBS scheme:
  - $ZKP_G Commit$
  - $ZKP_G Response$
  - $ZKP_G Verify$
- Own adaptation for short-term linkability:
  - $SignLinkable_G$
  - $VerifyLinkable_G$

# Procedures: $\text{KeyGen}_G(n)$

Generate group of  $n$  users and their respective set of keys.

- 1 select  $h \xleftarrow{R} G_1 \setminus \{1_{G_1}\}$
- 2 generate  $gmsk = (\xi_1, \xi_2)$  where  $\xi_1, \xi_2 \xleftarrow{R} \mathbb{Z}_p^*$
- 3 set  $u, v \in G_1$  such that  $u^{\xi_1} = v^{\xi_2} = h$
- 4 select  $\gamma \xleftarrow{R} \mathbb{Z}_p^*$
- 5 set  $w = g_2^\gamma$
- 6 generate  $\forall \mathcal{U}_i, 1 \leq i \leq n$ , an SDH tuple  $(A_i, x_i)$  by:
  - select  $x_i \xleftarrow{R} \mathbb{Z}_p^*$
  - set  $A_i \leftarrow g_1^{1/(\gamma+x_i)}$
  - $\gamma$  is the private master key of the group key issuer



# Procedures: $\text{Sign}_G(\text{gpk}, \text{gsk}[i], M)$ I

Given  $\text{gpk} = (g_1, g_2, h, u, v, w)$ ,  $\text{gsk}[i] = (A_i, x_i)$  and a message  $M \in \{0, 1\}^*$ , output a signature of knowledge

$\sigma = (T_1, T_2, T_3, c, s_\alpha, s_\beta, s_x, s_{\delta_1}, s_{\delta_2})$ .

- 1 select  $\alpha, \beta \xleftarrow{R} \mathbb{Z}_p$
- 2 compute the linear encryption of  $A$ :  $(T_1, T_2, T_3) \leftarrow (u^\alpha, v^\beta, Ah^{\alpha+\beta})$
- 3 compute  $\delta_1 \leftarrow x\alpha$  and  $\delta_2 \leftarrow x\beta$ ;
- 4 select  $r_\alpha, r_\beta, r_x, r_{\delta_1}, r_{\delta_2} \xleftarrow{R} \mathbb{Z}_p$
- 5 compute:
  - $R_1 \leftarrow u^{r_\alpha}$
  - $R_2 \leftarrow v^{r_\beta}$
  - $R_3 \leftarrow e(T_3, g_2)^{r_x} \cdot e(h, w)^{-r_\alpha - r_\beta} \cdot e(h, g_2)^{-r_{\delta_1} - r_{\delta_2}}$
  - $R_4 \leftarrow T_1^{r_x} \cdot u^{-r_{\delta_1}}$
  - $R_5 \leftarrow T_2^{r_x} \cdot v^{-r_{\delta_2}}$
- 6 compute:  $c \leftarrow H(M, T_1, T_2, T_3, R_1, R_2, R_3, R_4, R_5)$

# Procedures: $\text{Sign}_G(\text{gpk}, \text{gsk}[i], M) \parallel$

7 generate:

- $s_\alpha \leftarrow r_\alpha + c\alpha$
- $s_\beta \leftarrow r_\beta + c\beta$
- $s_x \leftarrow r_x + cx$
- $s_{\delta_1} \leftarrow r_{\delta_1} + c\delta_1$
- $s_{\delta_2} \leftarrow r_{\delta_2} + c\delta_2$

8 output  $\sigma \leftarrow (T_1, T_2, T_3, c, s_\alpha, s_\beta, s_x, s_{\delta_1}, s_{\delta_2})$ .

# Procedures: $\text{Verify}_G(\text{gpk}, M, \sigma)$

Given  $\text{gpk} = (g_1, g_2, h, u, v, w)$ , a message  $M$  and  $\sigma = (T_1, T_2, T_3, c, s_\alpha, s_\beta, s_x, s_{\delta_1}, s_{\delta_2})$ , verify that  $\sigma$  is a valid signature of the message

1 re-derive  $R_1, R_2, R_3, R_4, R_5$ :

- $\tilde{R}_1 \leftarrow u^{s_\alpha} / T_1^c$
- $\tilde{R}_2 \leftarrow v^{s_\beta} / T_2^c$
- $\tilde{R}_3 \leftarrow e(T_3, g_2)^{s_x} \cdot e(h, w)^{-s_\alpha - s_\beta} \cdot e(h, g_2)^{-s_{\delta_1} - s_{\delta_2}} \cdot (e(T_3, w) / e(g_1, g_2))^c$
- $\tilde{R}_4 \leftarrow T_1^{s_x} / u^{s_{\delta_1}}$
- $\tilde{R}_5 \leftarrow T_2^{s_x} / v^{s_{\delta_2}}$

2 verify  $c \stackrel{?}{=} H(M, T_1, T_2, T_3, \tilde{R}_1, \tilde{R}_2, \tilde{R}_3, \tilde{R}_4, \tilde{R}_5)$

# Procedures: $\text{Open}_{\mathcal{G}}(\text{gpk}, \text{gmsk}, M, \sigma)$

- Trace a signature to a concrete signer inside the group
- $\mathcal{M}_{\mathcal{G}}$  holds  $\text{gmsk}$  master key and knows all  $(A_i, x_i)$  pairs
- Given  $\text{gpk} = (g_1, g_2, h, u, v, w)$ ,  $\text{gmsk} = (\xi_1, \xi_2)$ , a message  $M$  and  $\sigma = (T_1, T_2, T_3, c, s_\alpha, s_\beta, s_x, s_{\delta_1}, s_{\delta_2})$ :
  - Recover user's identity:  $A \leftarrow T_3 / (T_1^{\xi_1} \cdot T_2^{\xi_2})$
  - If elements  $\{A_i\}$  of the  $\text{gsk}[i]$  are given to  $\mathcal{M}_{\mathcal{G}}$ , look up the user index for  $A$  recovered from the signature

# Procedures: $\text{SignLinkable}_G(\text{gpk}, \text{gsk}[i], M)$

Given  $\text{gpk}$ ,  $\text{gsk}[i]$ , a new message  $M'$ , a previous signature  $\sigma$ , and the values  $\alpha, \beta$  used for that signature, compute and output a signature  $\sigma'$

- First use: standard  $\text{Sign}_G(\text{gpk}, \text{gsk}[i], M)$ . Obtains  $\sigma$  with  $(\alpha, \beta)$
- Further uses:  $\text{SignLinkable}_G(\text{gpk}, \text{gsk}[i], M', \sigma, \alpha, \beta)$ :
  - 1 use the same pair  $(\alpha, \beta)$  producing the same linear encryption of  $A$ :  
 $(T_1, T_2, T_3) = (u^\alpha, v^\beta, Ah^{\alpha+\beta})$
  - 2 given a message  $M'$ , sign the message:  
 $\sigma' \leftarrow (T_1, T_2, T_3, c', s'_\alpha, s'_\beta, s'_x, s'_{\delta_1}, s'_{\delta_2})$  where  
 $c' \leftarrow H(M', T_1, T_2, T_3, R'_1, R'_2, R'_3, R'_4, R'_5) \in \mathbb{Z}_p$

# Procedures: $\text{VerifyLinkable}_G(\sigma, \sigma')$

This algorithm takes two signatures  $\sigma$  and  $\sigma'$  as input and outputs *true* or *false* depending on whether the signatures have been produced by the same signer's pseudonym:

- $T_1 \stackrel{?}{=} T_1'$
- $T_2 \stackrel{?}{=} T_2'$
- $T_3 \stackrel{?}{=} T_3'$

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# Requirements

- Authenticity
- Non-repudiation
- Integrity
- Revocable anonymity
- Short-term linkability
- Non-overspending
- Transferability



# Participants

- User ( $\mathcal{U}$ )
- Issuer ( $\mathcal{I}$ )
- Service provider ( $\mathcal{P}$ )
- Group Manager ( $\mathcal{M}_{\mathcal{G}}$ )

# Phases

- Ticket issue
- Ticket transfer
  - 1st time (from original)
  - Further times (from already transferred)
- Ticket verification
  - Standard (original)
  - Transferred
- Revocation of anonymity ( $\mathcal{M}_{\mathcal{G}}$ )

# Phases: Ticket issue

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**User ( $\mathcal{U}$ )**


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**Issuer ( $\mathcal{I}$ )**


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$$n_\alpha \xleftarrow{R} \mathbb{Z}_p$$

$$\longleftarrow n_\alpha$$

selects  $S_v$

$$V = \text{Sign}_G(S_v, n_\alpha, \text{flag\_issue})$$

$$\xrightarrow{V}$$

$$\text{Verify}_G(V)$$

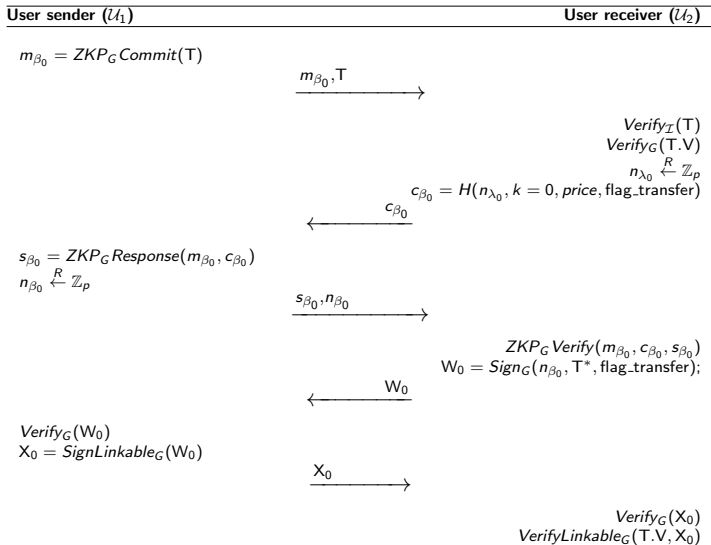
$$T = \text{Sign}_I(S_n, S_v, T_c, V, \dots)$$

$$\longleftarrow T$$

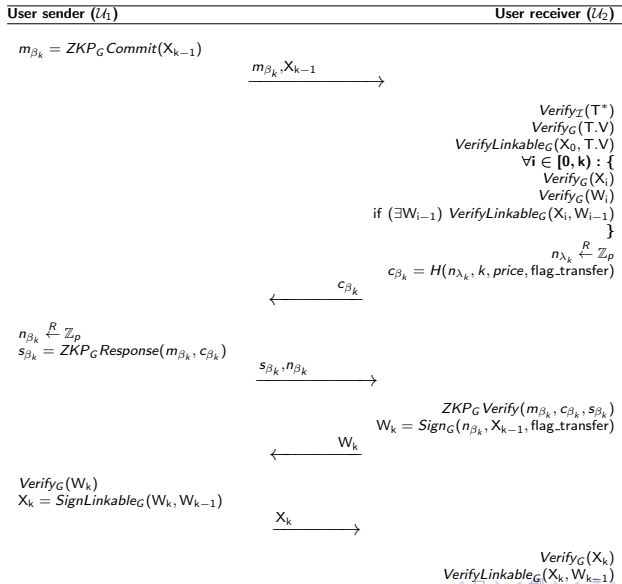
$$\text{Verify}_I(T)$$


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# Phases: Ticket transfer (1st time)



# Phases: Ticket transfer (further times)



# Phases: Ticket verification (standard)

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**User ( $\mathcal{U}$ )**


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**Provider ( $\mathcal{P}$ )**


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$$T^* \longrightarrow$$

$$\text{Verify}_{\mathcal{I}}(T^*)$$

$$\text{Verify}_{\mathcal{G}}(T.V)$$

$$n_{\gamma} \stackrel{R}{\leftarrow} \mathbb{Z}_p$$

$$\longleftarrow n_{\gamma}$$

$$Y = \text{SignLinkable}_{\mathcal{G}}(n_{\gamma}, T.Sn, \text{flag\_spend\_standard})$$

$$Y \longrightarrow$$

$$\text{Verify}_{\mathcal{G}}(Y)$$

$$\text{VerifyLinkable}_{\mathcal{G}}(T.V, Y)$$


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# Phases: Ticket verification (transferred)

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**User ( $\mathcal{U}$ )**


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**Provider ( $\mathcal{P}$ )**


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$$X_k \longrightarrow$$

$$\begin{aligned}
 & \text{Verify}_{\mathcal{I}}(T^*) \\
 & \text{Verify}_G(T.V) \\
 & \text{VerifyLinkable}_G(X_0, T.V) \\
 & \forall i \in [0, k] : \{ \\
 & \quad \text{Verify}_G(X_i) \\
 & \quad \text{Verify}_G(W_i) \\
 & \quad \text{if } (\exists W_{i-1}) \text{VerifyLinkable}_G(X_i, W_{i-1}) \\
 & \quad \} \\
 & n_\gamma \stackrel{R}{\leftarrow} \mathbb{Z}_p
 \end{aligned}$$

$$\longleftarrow n_\gamma$$

$$Y = \text{SignLinkable}_G(n_\gamma, T.Sn, \text{flag\_spend\_transferred})$$

$$Y \longrightarrow$$

$$\begin{aligned}
 & \text{Verify}_G(Y) \\
 & \text{VerifyLinkable}_G(W_k, Y)
 \end{aligned}$$


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# Phases: Revocation of anonymity

In case of controversy (e.g. overspending),  $\mathcal{M}_G$  could revoke the anonymity of the misbehavior by calling  $Open_G$  procedure



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# Conclusions & future work

- Proposal for e-ticketing system
  - Revocable anonymity
  - Short-term linkability
  - Transferability
- Adaptation of group signature scheme for partial linkability
- Security analysis
- Future work:
  - Automated validation tools for the proposal
  - Performance analysis of current proposal in real scenario (mobile devices)
  - Atomic verification (chain of signatures)
  - Comparison of performance results

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