

# On the Complexity of Aggregating Information for Authentication and Profiling

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# Outline

- 1 Motivation
  - Sharing Information
  - Relevant Work
- 2 Theory
  - Model Overview
  - NP-Complete
  - Pseudo-polynomial Time Solution
- 3 Experimental Results
  - Keystroke Authentication
  - Feature Selection

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# The Drug

- Social Networking: Communicate with
  - Relatives
  - Friends
  - Acquaintances
  - Strangers
- Convenient (and quite useful)
- ... but sometimes too convenient.

twitter



LinkedIn

Google+

Blogger



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# The Abuser

- People often reveal too much information...
- across numerous sites.
- Intentional: User doesn't care or think of consequences
- Unintentional: Didn't read the fine-print
- No control: Stolen information... or even friends.

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5. Content you share with others
6. Other rules you set
7. Other rules you set
8. Other rules you set
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## Happy Birthday

**Alice:** posted on 2011/09/15  
Happy 40th Birthday, Bob!

**Bob:** posted on 2011/09/15  
Thanks! Why not just go ahead and tell everyone my Bank Account Number too.

**Alice:** posted on 2011/09/15  
Um, ok.



# The Collector

- Aggregates that information
- Generates profile of user(s)
- Examples:
  - Police (criminal inv.)
  - Business (ad. revenue)
  - Employer (security)



Google

BOEING



# The Collector's Intent

The collector's intent could be

- **Malicious (to the individual):**
  - No concern for individual's privacy.
  - Concern for best profile information.
- **Ambivalent:**
  - No malicious intent. Simply wants a good profile.
  - Still often disregards individual's privacy, or treats as secondary.
- **Benevolent:**
  - Individual privacy a top priority.
  - Wishes to maximize profile information while respecting privacy.



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# Examples

## Malicious

### Stealing Reality by Altschuler et al. [1]

- Malware threat that steals personal and behavioral info.
- Not just email addresses, passwords, phone numbers, etc.
- Gets static info: birthdate, mother's maiden name.
- Challenge: Very hard to change once acquired.

[1] Y. Altschuler, N. Aharoni, Y. Elovici, A. Pentland, and M. Cebrian. Stealing reality. Tech. rep., arXiv, October 2010. arXiv:1010.1028v1

# Examples

## Benevolent

*PerGym* by Pareschi et al. [2]

- Provides context-aware personalized services... while maintaining strong system security.
- Gym service: monitors workout experience, e.g.
  - Body temperature, Location, Mood
- User wishes to use service but does not trust enough to provide all info.

[2] L. Pareschi, D. Riboni, A. Agostini, and C. Bettini. Composition and generalization of context data for privacy preservation. *Sixth Annual IEEE International Conference on Pervasive Computing and Communications (PerCom 2008)*, pp. 429–433, March 2008, <http://dx.doi.org/10.1109/PERCOM.2008.47>



# Examples

## Ambivalent

### User authentication

- Old school: Password
- Biometrics: fingerprint, voice, face, typing pattern
- Multiple: Password, voice, *and* fingerprint scan
- System needs to collect biometric information.
- User might not want system to store all such information.

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# Relevant Work

- Carminati et al. [3] provide model to give user strong control over access to private info.
- Gambs et al. [4] discuss how geolocated applications (Google Latitude) enable a user to reveal too much personal info by sharing positional and mobility info.

[3] B. Carminati, E. Ferrari, and A. Perego. Enforcing access control in web-based social networks. *ACM Trans. Inf. Syst. Secur.* 13:6:1–6:38, November 2009, <http://doi.acm.org/10.1145/1609956.1609962>

[4] S. Gambs, M.-O. Killijian, and M. N. del Prado Cortez. Show me how you move and I will tell you who you are. *Transactions on Data Privacy* 4(2):103–126, 2011



# Relevant Work

- Liu and Terzi [5] estimate user's privacy score from info they provide online, notifying user if it exceeds selected threshold. (Like credit score/credit watch)
- Domingo-Ferrer [6] discuss trade-offs between privacy and functionality: cooperation while preventing “free rides”

[5] K. Liu and E. Terzi. A framework for computing the privacy scores of users in online social networks. *ACM Trans. Knowl. Discov. Data* 5:6:1–6:30, December 2010, <http://doi.acm.org/10.1145/1870096.1870102>

[6] J. Domingo-Ferrer. Rational privacy disclosure in social networks. *Modeling Decisions for Artificial Intelligence*, vol. 6408, pp. 255–265. Springer Berlin / Heidelberg, Lecture Notes in Computer Science, 2010, [http://dx.doi.org/10.1007/978-3-642-16292-3\\_25](http://dx.doi.org/10.1007/978-3-642-16292-3_25)



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# Model Assumptions

User has

- collection of private info (facts)

$$S = \{f_1, f_2, \dots, f_n\},$$

- weights - importance of each fact, and
- a notion of acceptable privacy based on combination of these weights.

# Model Assumptions

## Aggregator has

- algorithm to generate profile from given subset of  $S$
- including a (confidence/quality) score,
- minimum score threshold (valid/acceptable profile), and
- costs associated with collection of each fact.
  - Home address and phone number purchased by phonebook database.
  - Birth dates might require thorough searching of public birth records or social engineering.
  - Fingerprint relatively inexpensive.
  - DNA sample might be a bit more costly (and intrusive).



# Model Assumptions

## Benevolent aggregator

Success: if can find a subset of facts generating acceptable profile while not exceeding user's privacy threshold or possible collection cost limits.

## Malicious aggregator

Same but simply ignores privacy threshold, and would still be bound by cost limitations.



# Model Assumptions

- Given set  $S$  of facts
- Find subset  $S' \subseteq S$
- Given profile function  $F^p(S')$  and threshold  $T^p$ :  
Measure score of profile using  $S'$
- Given privacy function  $F^u(S')$  and threshold  $T^u$ :  
Measure user's privacy score of having revealed  $S'$
- Given cost function  $F^c(S')$  and threshold  $W$ :  
Cost of acquiring  $S'$
- A subset  $S'$  yields *valid* profile if  $F^p(S') \geq T^p$  and  $F^u(S') \leq T^u$  (for benevolent aggregators).



# Goal and Problems

## Goal

Analyze complexity of determining what information of a user is most valuable to collect given acquisition costs to create an acceptable (valid) profile.

## Problems

- More information does not nec. mean better profile
- Valuable but costly info
- Incorrect or contradictory info
- Value of item might depend on other info as well

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# Profile Aggregator Problem

## Theorem 1

Given

- a set  $S$  of facts,
- a cost function  $F^c$ , a cost goal  $W$ ,
- profiling function  $F^p$ , and confidence threshold  $TP$ ,

NP-C to determine if exists valid  $S' \subseteq S$  s.t.  $F^c(S') \leq W$ .

That is, (most likely) no polynomial-time algorithm exists that can select sufficient info (valid profile) while minimizing cost.

Since this holds when ignoring privacy function, it also holds with privacy function.

## Proof

Due to a reduction from the classic 0-1 Knapsack problem.



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# Pseudo-polynomial Time Solution: 0-1 Knapsack

- Given  $n$  items, with value  $v_i$  and weight  $w_i$ ,
- find a subset of items such that
  - total weight is below some limit  $W$  and
  - total value is as large as possible.
- Though NP-complete, pseudo-poly solution exists using dynamic programming.
- Time is  $O(nW)$  - thus polynomial in  $W$ .
- Result works because adding an item  $i$ , increases the total value by  $v_i$  and the total weight by  $w_i$ .
- That is, the value and weight functions are monotonic.
- In our setting, the weight function is the cost function  $F^C$  and the value function is the profile function  $F^P$ .
- Thus...



# Pseudo-polynomial Time Solution: Profile Aggregator

## Theorem 2

*Given*

- *a set  $S$  of facts,*
- *a monotonic cost function  $F^c$ , a cost goal  $W$ ,*
- *a monotonic profiling function  $F^p$ , and confidence threshold  $T^p$ .*

*One can determine in time  $O(nW)$  if there exists valid  $S' \subseteq S$  such that  $F^c(S') \leq W$ .*

(Note this only applies to the case when privacy is ignored.)



# Pseudo-polynomial Time Solution: Profile Aggregator

## Theorem 2

*Given*

- a set  $S$  of facts,
- a monotonic cost function  $C$  and cost goal  $W$ ,
- a monotonic profiling function  $F^P$ , and confidence threshold  $T^P$ .

*One can determine in time  $O(nW)$  if there exists valid  $S' \subseteq S$  such that  $F^C(S')$*

*(Note this only applies to the case when privacy is ignored.)*

LIE LIE LIE LIE



# Monotonic versus Consistently Monotonic

## Monotonic

A function is **monotonic** if for two subsets  $A$  and  $B$ ,  $F(A) \leq F(A \cup B)$ . That is, adding elements to a subset will never decrease the score.

## Consistently Monotonic

A function is **consistently monotonic** if for three subsets  $A$ ,  $B$ , and  $C$ ,  $F(A) \leq F(B) \rightarrow F(A \cup C) \leq F(B \cup C)$ . That is, if the score for  $A$  is lower than for  $B$  then adding  $C$  to both sets will not change this order.



# Monotonic versus Consistently Monotonic

## Informal Example

- Assume one is going backpacking across Europe
- and has to choose among several food staples  
(just a subset here.)
  - A. Potato Chips
  - B. Canned food
  - C. Can opener
- If choosing just one item, we have a clear winner -  $F(A)$  is going to be better than the other two.
- Adding any item does not decrease score - so *monotonic*.
- However, although  $F(B) \leq F(A)$ , clearly (for health reasons)  $F(B \cup C) > F(A \cup C)$  - so *not consistently monotonic*.



# Monotonic versus Consistently Monotonic

## One more issue

- Dynamic programming solution requires that values for the cost function be nonnegative integers.
- Or else it cannot store all possible cost values.
- Can scale if within a known fractional range.
- For simplicity, assume purely a summation of costs.



# Pseudo-polynomial Time Solution: Profile Aggregator

## Theorem 2

*Given*

- a set  $S$  of facts,
- a set of integer costs  $c_s$ , one per fact  $s$ , a cost goal  $W$ ,
- a consistently monotonic profiling function  $F^P$  and  $T^P$ .

Can see in time  $O(nW)$  if there exists valid  $S' \subseteq S$  such that  $\sum_{s \in S'} c_s \leq W$ .

(Note this still only applies to the case when privacy is ignored.)

## ***Theorem 3 (Monotonic case):***

When  $F^P$  is merely monotonic, NP-complete even if  $W \in \Theta(n^k)$ .

Reduction from the Vertex-Cover Problem.

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# Justification

- Increasing the number of facts collected (and used) does not necessarily improve profile generated.
- In fact, it may hurt it... significantly.
- Do an experiment to see this.



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# Keystroke Authentication

- Traditional Authentication: User enters a password and system checks if password matches.
- Here: Authentication system collects (and verifies) password but also collects keystroke information, namely:
  - Key hold latencies: press to release of same key
  - Key interval latencies: release to press of new key
  - Key press latencies: press of one key to the next
- User authenticates if enters correct password *and* keystroke pattern best matches claimed user's.

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# Keystroke Authentication

- Our data consists of 43 users entering a 37-character phrases (repeatedly - 9 times).
- 37 characters means we had  $37 \cdot 3 - 2 = 109$  features.
- Each feature represents one dimension in 109-d space.
- Contains  $43 \cdot 9 = 387$  points in this space.





# Classification

Process works as follows:

- Train on a sample of the data set - creating a classification system.
- For a test point, query the system to identify to which user class this point most likely belongs.
- If it matches the known user for this query, considered a correct match; otherwise, considered an error.
- Used LOOCV (leave-one-out cross validation) scheme, training data is all but one item (the test query).



# Classification

Process works as follows:

- For given training set and a subset of 109 features,
- build classifiers on feature subset for this training set.
- A successful profile is one where the user matches.
- The confidence in our profile function is the accuracy it is estimated to predict correctly.
- $F(S')$  is the accuracy of classifier, as measured by percentage of correct classifications.
- Wish to identify the subset that maximizes this function. Thus, classifier remains fixed but features to train vary.



# Classification

Process works as follows:

- Trying all possible  $2^{109}$  subsets of features is infeasible.
- Heuristics would likely do well but our goal is to “justify that more is not always better” and to stress the importance of selecting a good subset.
- Not to discover the best way to find a subset.
- We also chose to use the weighted  $k$ -nearest neighbors classifier
  - for its simplicity and
  - decent classification abilities.
  - By no means is this an optimal classifier.



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# Experiment

- LOOCV
- k-NN classifier
- Best subset of 109 features
- Profiling function is too complicated to analyze directly and in fact depends on the training data.
- Two approaches to choosing features:
  - Dynamic programming:
    - even though do not know if function is cons. monotonic.
  - Sequential approach (in order until "full"):
    - For comparison and to help see property of the function.
- Ran two versions of experiment:
  - with equal (unit) weights per feature.
    - Cost for using  $k$  features is  $k$ .
  - with weight growing linearly based on character position.
    - Reflects user exhaustion - longer sequences, higher cost.

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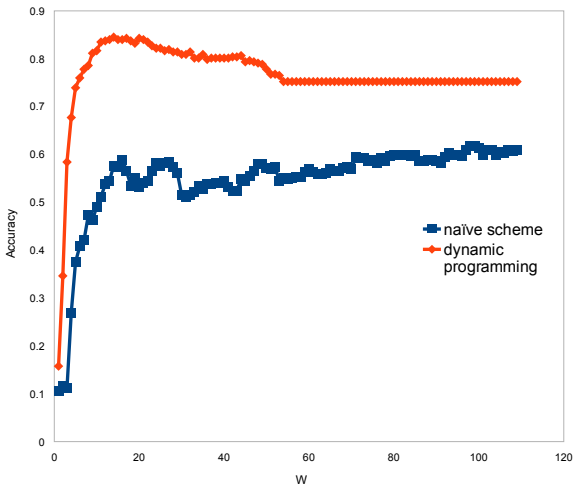
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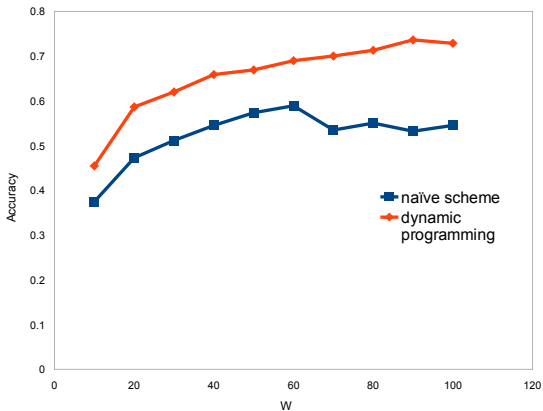
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# Experiment (Equal Weights)



# Experiment (Increasing Weights)



# Summary

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- Minimizing cost/maximizing profit - difficult in theory  
*Not surprising*
- The properties of profit function affect difficulty  
*Not surprising*
- Being monotonic isn't particularly helpful but being consistently monotonic is.  
*Surprising?*
- Picking correct subset of information is important  
More is definitely not always better
- Future Outlook
  - Study other (real) classifiers: even better improvements?
  - Study heuristical means of selecting features: comparison to DP version

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- Minimizing cost/maximizing profit - difficult in theory  
*Not surprising*
- The properties of profit function affect difficulty  
*Not surprising*
- Being monotonic isn't particularly helpful but being consistently monotonic is.  
*Surprising?*
- Picking correct subset of information is important  
More is definitely not always better
- Future Outlook
  - Study other (real) classifiers: even better improvements?
  - Study heuristical means of selecting features: comparison to DP version



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Any Questions?

